

## DISCOVERY OF A RINGLIKE DARK MATTER STRUCTURE IN THE CORE OF THE GALAXY CLUSTER Cl 0024+17

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*Received 2006 September 6; accepted 2007 March 2*

### ABSTRACT

We present a comprehensive mass reconstruction of the rich galaxy cluster Cl 0024+17 at  $z \simeq 0.4$  from ACS data, unifying both strong- and weak-lensing constraints. The weak-lensing signal from a dense distribution of background galaxies ( $\sim 120 \text{ arcmin}^{-2}$ ) across the cluster enables the derivation of a high-resolution parameter-free mass map. The strongly lensed objects tightly constrain the mass structure of the cluster inner region on an absolute scale, breaking the mass-sheet degeneracy. The mass reconstruction of Cl 0024+17 obtained in such a way is remarkable. It reveals a ringlike dark matter substructure at  $r \sim 75''$  surrounding a soft, dense core at  $r \lesssim 50''$ . We interpret this peculiar substructure as the result of a high-speed line-of-sight collision of two massive clusters  $\sim 1\text{--}2$  Gyr ago. Such an event is also indicated by the cluster velocity distribution. Our numerical simulation with purely collisionless particles demonstrates that such density ripples can arise by radially expanding, decelerating particles that originally comprised the precollision cores. Cl 0024+17 can be likened to the bullet cluster 1E 0657–56, but viewed *along* the collision axis at a much later epoch. In addition, we show that the long-standing mass discrepancy for Cl 0024+17 between X-ray and lensing can be resolved by treating the cluster X-ray emission as coming from a superposition of two X-ray systems. The cluster’s unusual X-ray surface brightness profile that requires a two isothermal sphere description supports this hypothesis.

*Subject headings:* cosmology: observations — dark matter — galaxies: clusters: individual (Cl 0024+17) — galaxies: high-redshift — gravitational lensing — X-rays: galaxies: clusters

*Online material:* color figure

### 1. INTRODUCTION

A galaxy cluster is still growing in today’s universe by continuously accreting other clusters/groups of galaxies. Because the cluster and the infalling object are likely to reside in a common filament, their relative motions are predominantly expected to be one-dimensional (i.e., along the filament). This makes cluster cores the busiest places in cluster dynamics subject to frequent near head-on collisions. Because the universe is not old enough to completely virialize these ever-growing clusters, many cluster cores are believed to maintain bulk properties reflecting the cluster formation history even in the low- $z$  universe.

Recently, there have been a number of reports on the detection of such clusters especially from X-rays (e.g., Mazzotta et al. 2001; Vikhlinin et al. 2001; Markevitch et al. 2002; Dupke & White 2003; Henry et al. 2004; Belsole et al. 2005; Ferrari et al. 2006). Most of these clusters are characterized by distinct discontinuities in temperature or density gradient of the intracluster medium (ICM). However, these X-ray features hinting at the previous merging history are hard to identify if the collision is in progress along the line of sight. Numerical simulations predict

that in such a configuration the disruption of the ICM is azimuthally symmetric and thus the ICM of the cluster may appear spherically relaxed with radial temperature gradients (e.g., Takizawa 2000), which cannot be easily disentangled from the intrinsic temperature gradient for a single relaxed system. In the current paper we study one such case, namely, Cl 0024+17, with gravitational lensing using deep Advanced Camera for Surveys (ACS) observations.

Since its discovery by Humason & Sandage (1957), the intermediate-redshift ( $z = 0.4$ ) cluster Cl 0024+17 has been a target of a number of studies (e.g., Zwicky 1959; Gunn & Oke 1975; Koo 1988; Kassiola et al. 1992; Bonnet et al. 1994; Smail et al. 1996; Colley et al. 1996; Tyson et al. 1998; Dressler et al. 1999; Broadhurst et al. 2000; Shapiro & Iliev 2000; Soucail et al. 2000; Czoske et al. 2001; Kneib et al. 2003; Ota et al. 2004; Zhang et al. 2005; Metevier et al. 2006). One of the most puzzling problems in Cl 0024+17 is the large mass discrepancy between the X-ray and the lensing results in the cluster core. The five prominent arcs with a spectroscopic redshift of 1.675 (Broadhurst et al. 2000) at  $r \sim 30''$  from the cluster center have prompted many authors to model the mass distribution in the central region (e.g., Colley et al. 1996; Tyson et al. 1998; Broadhurst et al. 2000; Comerford et al. 2006). Although the mass estimates and density profiles from these authors are at slight variance with one another, it is evident that the lensing analyses yield systematically higher core masses than the X-ray results by a factor of 3–4 (Ota et al. 2004; Zhang et al. 2005). Because the five multiple images are well resolved and the proposed mass models can successfully predict the location, orientation, and parity of the five lensed images, the discrepancy has been attributed to problems in X-ray mass estimation due to a severe departure from the hypothesized hydrostatic equilibrium.

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One of the most convincing pieces of evidence for the recent dynamical disruption in the cluster center (i.e., responsible for the departure from the equilibrium) comes from the study of the cluster velocity field by Czoske et al. (2002). From  $\sim 300$  objects in the redshift range  $0.37 < z < 0.42$ , they find that the redshift distribution is bimodal, showing two clear peaks at  $z = 0.381$  and  $0.395$ . By investigating the radial distribution of the velocity field of these two populations, they argue that the system has undergone a high-speed line-of-sight collision of two massive subclusters. Their numerical simulation with a mass ratio of about 2:1 reproduces the observed pattern of the velocity field. If we are indeed observing a superposition of two clusters, the lensing mass should be the sum of the two components. On the other hand, the X-ray mass estimation by the previous authors (e.g., Ota et al. 2004; Zhang et al. 2005) assumes a single component although the collision scenario by Czoske et al. (2002) is acknowledged. The validity of treating the X-ray emission as coming from a single X-ray system, of course, depends on the state of the merger. If the two ICM systems have already merged and settled down to an equilibrium state, the observed temperature and the slope of the profile can be viewed as representing the global properties of the relaxed postmerger system. However, if we are observing two postcollision clusters that are still separated, the single-component assumption should lead to a substantial underestimation of the projected mass.

Gravitational lensing has been claimed to be a unique method to measure mass properties of an object free from any dynamical assumption. However, although it is true that the lensing signal does not depend on the composition or the temperature of the deflector, in practice this “assumption-free” statement can be warranted only when a sufficient number of lensing features are observable.

If the signal is sparse, a lensing mass reconstruction inevitably necessitates some assumptions. Whether or not these assumptions are more dangerous than the quasi-equilibrium hypothesis in X-ray approaches certainly relies on the complexity of an individual system, as well as the number of observables. In this respect, mass reconstructions of Cl 0024+17 solely based on a limited number of multiple images are unwarranted despite the well-resolved morphology of the lensed images. In principle, any curl-free vector field (i.e., gradient of a scalar potential) that correctly predicts the known multiple images can be suggested as a deflection field of the system (surface mass density can be later derived by taking the divergence of this deflection field). Because the location and shape of the source is unknown and the rest of the region not occupied by the multiple images cannot be constrained, the solution is indeterminate. The situation can be slightly alleviated if some physical considerations are used as additional constraints such as smoothness of mass distribution, resemblance of dark matter distribution to cluster galaxy distribution, analytic behavior of density profiles (e.g., Navarro et al. 1997), etc. These assumptions are often implemented by placing parameterized dark matter halos on top of bright cluster ellipticals. Nevertheless, the previous models in the literature (e.g., Tyson et al. 1998; Broadhurst et al. 2000; Comerford et al. 2006), although all successful in predicting the multiple images, show somewhat discrepant mass distributions. This is not surprising because even with the help of those assumptions, one still faces many ambiguities, such as where to place what types of dark matter halos.

Therefore, in the current investigation, we aim to present a parameter-free<sup>7</sup> mass reconstruction of Cl 0024+17 combining

multiply lensed images and the ellipticities of  $\sim 1300$  background galaxies. Several papers have already discussed this idea of unifying strong- and weak-lensing data in a parameter-free cluster mass reconstruction and applied the concept to observations (e.g., Abdelsalam et al. 1998; Bridle et al. 1998; Seitz et al. 1998; Kneib et al. 2003; Smith et al. 2005; Bradač et al. 2005; Diego et al. 2007; Halkola et al. 2006; Cacciato et al. 2006). The approach used in the current study is similar to the ones investigated by Bridle et al. (1998), Seitz et al. (1998), and Bradač et al. (2005), who proposed to model a cluster mass distribution by setting up a two-dimensional grid over the cluster field. We discuss the details of the method and the differences from the previous techniques in § 3.

This approach utilizes information available in the entire cluster field and is also assumption-free, completely blind to the distribution of the baryonic component of the cluster. Because the ACS on board the *Hubble Space Telescope* (HST) can resolve very faint, but highly distorted, distant galaxies, the number density of the available source galaxies is unprecedentedly high. In addition, the deep, six-passband coverage from F435W to F850LP provides secure photometric redshifts for individual objects, allowing us not only to select the source population efficiently with a minimal dilution of the lensing signal from non-background galaxies, but also to properly weight their lensing efficiency according to their cosmological distances. The resulting mass map obtained in this way will not be limited by a particular parameterization and will reveal any significant substructure if the cluster core has indeed undergone a violent recent line-of-sight collision.

We organize our analyses as follows. In § 2 we describe the observational aspects including basic data reduction, photometric redshift estimation, point-spread function (PSF) correction, ellipticity measurement, etc. The basic theory and algorithm of our parameter-free mass reconstruction are discussed in § 3. In § 4 we present the result of the gravitational lensing analysis of Cl 0024+17. The result is discussed in § 5, before the conclusion in § 6.

Throughout the paper we assume the  $\Lambda$ CDM cosmology with  $\Omega_M = 0.27$ ,  $\Omega_\Lambda = 0.73$ , and  $H_0 = 71 \text{ km s}^{-1} \text{ Mpc}^{-1}$ . All the quoted uncertainties are at the  $1 \sigma$  level ( $\sim 68\%$ ). We define the ellipticity as  $(a - b)/(a + b)$ , where  $a$  and  $b$  are the major and minor axes of the object, respectively.

## 2. OBSERVATIONS

### 2.1. Data Reduction and Photometry

The intermediate-redshift cluster Cl 0024+17 at  $z = 0.395$  was observed with the Wide Field Channel (WFC) of the ACS in 2004 November as part of our Guaranteed Time Observations (GTO; ID 10325). A single pointing ( $\sim 3.3' \times \sim 3.3'$  field of view) is centered at the cluster core ( $\alpha_{J2000.0} \simeq 00^{\text{h}}26^{\text{m}}35^{\text{s}}$ ,  $\delta_{J2000.0} \simeq 17^{\circ}09'43''$ ) with integrations of 6435, 5072, 5072, 8971, 10,144, and 16,328 s in the F435W, F475W, F555W, F625W, F775W, and F850LP<sup>8</sup> filters, respectively. The low-level CCD processing (e.g., overscan/bias subtraction, flat-fielding) was carried out using the STScI standard ACS calibration pipeline (CALACS; Hack et al. 2003), whereas the final high-level processing (e.g., geometric distortion correction, cosmic-ray removal, image mosaicking) was performed with the ACS GTO pipeline “Apsis” (Blakeslee et al. 2003). The integrity of the

<sup>7</sup> In this paper we use the term “parameter-free” or “nonparametric” mass reconstruction to refer to a grid-based method. It is trivially obvious that the method also needs a set of “parameters” to define the grid.

<sup>8</sup> These F435W, F475W, F555W, F625W, F775W, and F850LP filters are commonly referred to as  $B_{435}$ ,  $g_{475}$ ,  $V_{555}$ ,  $r_{625}$ ,  $i_{775}$ , and  $z_{850}$ , respectively. We follow this convention hereafter.



FIG. 1.—*HST* ACS color composite of Cl 0024+17 in the observed orientation: north is right and east is up. The ACS WFC  $g_{475}$ ,  $r_{625}$ , and  $z_{850}$  images are used to represent the intensities in blue, green, and red, respectively. We show the central square ( $196'' \times 196''$ ) region of the cluster, which precisely overlaps our mass reconstruction field. The five multiple images of the single source at  $z = 1.675$  are labeled as A1–A5. We also denote the two other multiple-image system candidates (see § 3.2) by B1–B2 and C1–C2.

image alignment carried out by Apsis has been extensively tested in our previous weak-lensing analyses (Jee et al. 2005a, 2005b, 2006; Lombardi et al. 2005). We used the Lanczos3 (windowed sinc function) kernel in drizzling (Fruchter & Hook 2002), which produces a sharper PSF and less noise correlation between adjacent pixels than a “square” kernel (for more detailed description of the noise and aliasing properties of Lanczos3 vs. other drizzle interpolation kernels see Mei et al. 2005).

In Figure 1 we present the color composite of the cluster field created from these final Apsis products. The image is displayed in the observed orientation (north is right and east is up) and is made square by trimming the four sides of the original to match our mass reconstruction field. The blue, green, and red intensities are represented with the  $g_{475}$ ,  $r_{625}$ , and  $z_{850}$  fluxes, respectively. The well-known five multiple images at  $z = 1.675$  are labeled as A1–A5. We also denote the two other multiple-image system candidates (see § 3.2) by B1–B2 and C1–C2.

Because “drizzling” correlates pixel noise, one must use caution in producing the rms maps for the final photometry. Apsis correctly calculates the rms for each pixel in the absence of this correlation. We created a detection image by weight-averaging all bandpass images using their inverse variance maps. Objects were detected with SExtractor by searching for at least five connected pixels above 1.5 times sky rms. We manually removed  $\sim 330$  spurious objects (e.g., diffraction spikes around bright stars, uncleaned cosmic rays near the field boundaries). We note that some giant arcs and bright spirals are undesirably fragmented and identified as multiple objects by SExtractor. For these objects, we merged their segmentation map pixels by hand and performed photometry by running SExtractor via the SExSeg software (Coe et al. 2006).

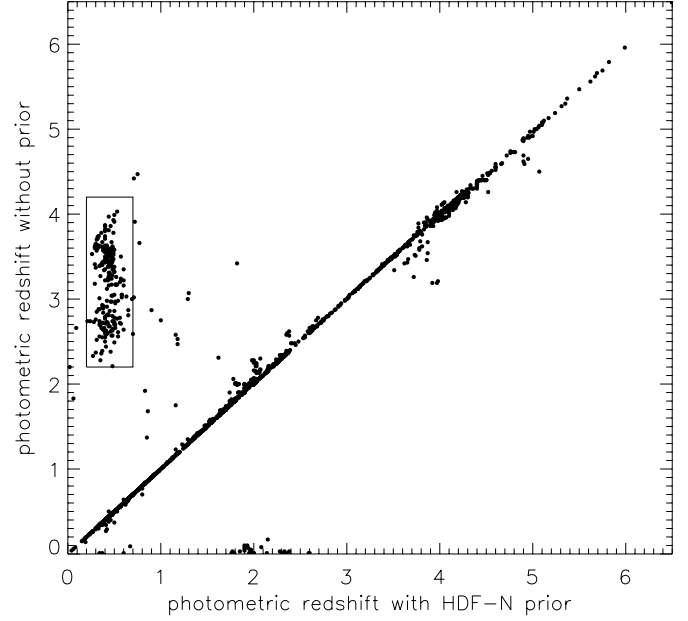


FIG. 2.—Effects of priors in the photometric redshift estimation. We produce two sets of photometric redshift catalogs to examine the effect of the HDF-N prior in the presence of lensing. The comparison shows that no systematic difference is found between the two sets except for those objects in the box. It appears that these objects are associated with the main cluster at  $z \sim 0.4$  but are mistaken for high-redshift objects when no prior is used.

## 2.2. Photometric Redshift and Selection of Background Galaxies

Our deep, six-passband coverage of the cluster allows us to obtain secure photometric redshifts of objects in the Cl 0024+17 field. We used the isophototal magnitudes output by SExtractor to compute galaxy colors and ran the revised Bayesian Photometric Redshift code (BPZ; Benítez 2000; Benítez et al. 2004) to determine their photometric redshifts. The four spectral energy distribution (SED) templates of E, Sbc, Scd, and Im by Coleman et al. (1980) and the two starburst templates of SB2 and SB3 by Kinney et al. (1996) are employed. As described in Benítez et al. (2004), the slopes of the SED were modified to give agreement with the Hubble Deep Field (HDF) spectroscopic redshifts. We also attempted to further calibrate the zero points of the photometry with the publicly available spectroscopic redshift catalog of the Cl 0024+17 field (Moran et al. 2005). However, we found that the estimated offsets are very small (we obtained 0.001,  $-0.012$ , 0.005, 0.013, 0.005, and  $-0.009$  for the  $B_{435}$ ,  $g_{475}$ ,  $V_{555}$ ,  $r_{625}$ ,  $i_{775}$ , and  $z_{850}$  filters, respectively) and the final result is not affected. The postlaunch sensitivity curves of ACS by Sirianni et al. (2005) are used to obtain synthetic photometry of these templates from  $z = 0.01$  to 6 at a redshift interval of  $\Delta z = 0.01$ . BPZ then compares this synthetic photometry to the observed photometry to determine the redshift probability distribution for each galaxy. The strength of BPZ lies in its use of priors; each galaxy is assigned a prior redshift probability distribution based on its magnitude. This prior is multiplied by the probability obtained from the photometric SED fitting. However, in these Cl 0024+17 images, the magnitudes of background objects are magnified by the cluster lensing. Thus, each background galaxy will be assigned a slightly biased prior.

To test the effects of the prior, we generated two sets of photometric redshift catalogs with and without priors obtained from the Hubble Deep Field–North (HDF-N) photometric redshift distribution. However, as demonstrated in Figure 2, we do not

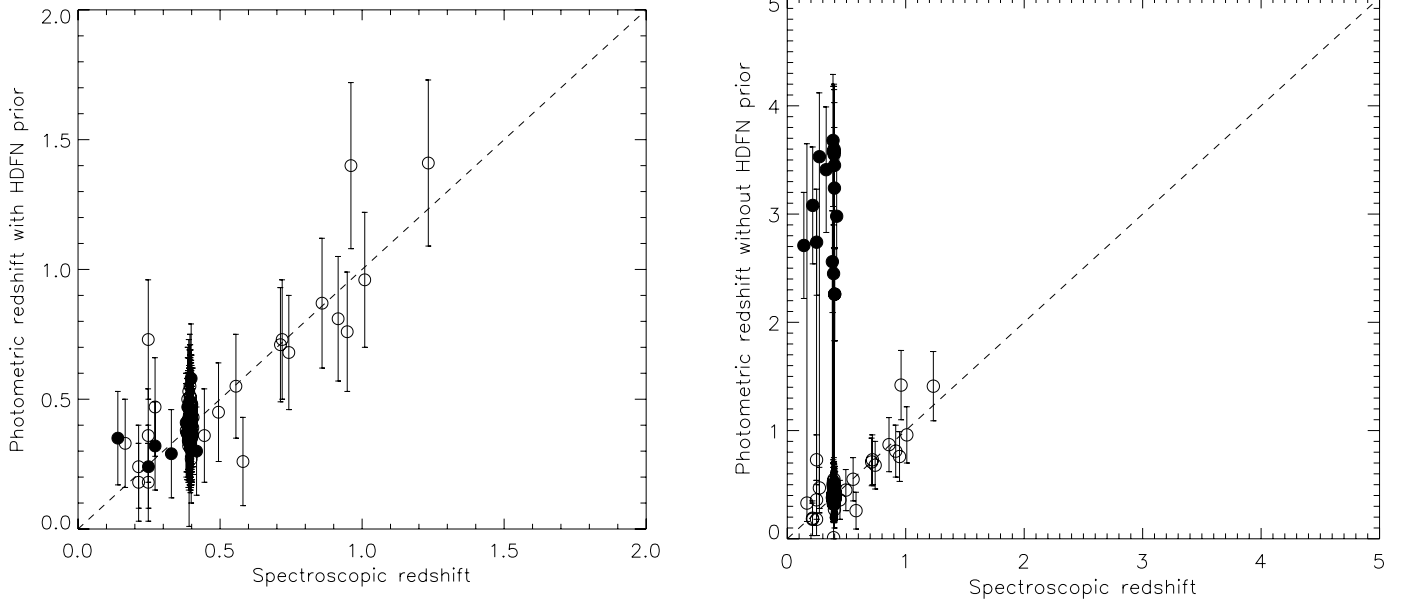


FIG. 3.—Spectroscopic redshifts vs. photometric redshifts. The photometric redshifts obtained with HDF-N priors are consistent with the spectroscopic redshifts (*left*). The filled circles correspond to the objects classified as outliers in the right panel. When the photometric redshifts are computed without priors, we observe catastrophic outliers at  $z_{\text{phot}} = 2-4$  (see the text for description).

observe any systematic difference between these two sets except for the objects within the box. The photometric redshifts of these objects obtained with HDF-N priors have a mean of  $z \sim 0.4$  with a dispersion of  $\Delta z \sim 0.2$ , whereas the photometric redshift estimation without priors identifies them as high-redshift objects at  $2 \lesssim z \lesssim 4$ . Many of these galaxies appear to have early-type morphology. This suggests that a substantial fraction of the population is either associated with Cl 0024+17 or at lower redshifts, and their redshifts are correctly estimated only with the help of priors.

The comparison of our photometric redshifts with the publicly available spectroscopic redshifts compiled by Moran et al. (2005) strongly supports this hypothesis (Fig. 3). The catalog contains 142 objects within our ACS field. Our photometric redshifts with HDF-N priors are consistent with the spectroscopic results as shown in the left panel of Figure 3, whereas the photometric redshifts computed without priors produce the catastrophic outliers at  $2 < z < 4$  (*filled circle in the right panel*).

The reasons that these objects are mistaken for high-redshift objects are as follows. Because we estimate SEDs of galaxies using broadband photometry without UV and near-infrared data, some degeneracies are inevitable. Especially, when there are some residual UV fluxes, the 4000 Å break feature becomes weak and can be confused with other spectral features at high redshifts; these degeneracies are worsened by photometric errors for faint galaxies. The typical shape of the redshift probability distribution of these objects has two dominant peaks: one at  $z \sim 0.4$  and the other at  $z = 2-4$ . In cases where the peak at  $z = 2-4$  is greater than the peak at  $z \sim 0.4$ , BPZ gives the former when no prior is used. However, if the probability distribution is multiplied by the prior and the  $z \sim 0.4$  peak now becomes the greater of the two, the BPZ output is  $z \sim 0.4$ . Of course, the interpretation is that the object is “too bright” to be placed at  $z = 2-4$ .

Benítez et al. (2004) also showed in their photometric redshift estimation with the WFPC2 *BVI* photometry that without prior the typical SED fitting method produces outliers at  $z = 2-4$ . The cloud of points at  $z = 2-4$  in Figure 14 of Benítez et al. (2004) somewhat resembles the  $z = 2-4$  outliers in our

paper (see also Fig. 19 of Coe et al. [2006], which visually illustrates one such degeneracy in the SED fitting).

Because no significant systematic discrepancy is found in other redshift ranges, we justify the use of HDF-N priors without any modification of the existing code. We show the photometric redshift distribution of  $\sim 1820$  ( $i_{775} < 27.5$ ) nonstellar objects obtained with HDF-N priors in the cluster field in Figure 4. The redshift spike at  $z = 0.4$  (*dotted line*) is clearly visible.

For our mass reconstruction of the cluster, we select objects whose photometric redshifts are greater than  $z = 0.8$  with a minimum detection significance of  $5\sigma$  at least in one filter. These conservative values are chosen to ensure that the selection suffers from minimal contamination by nonbackground population

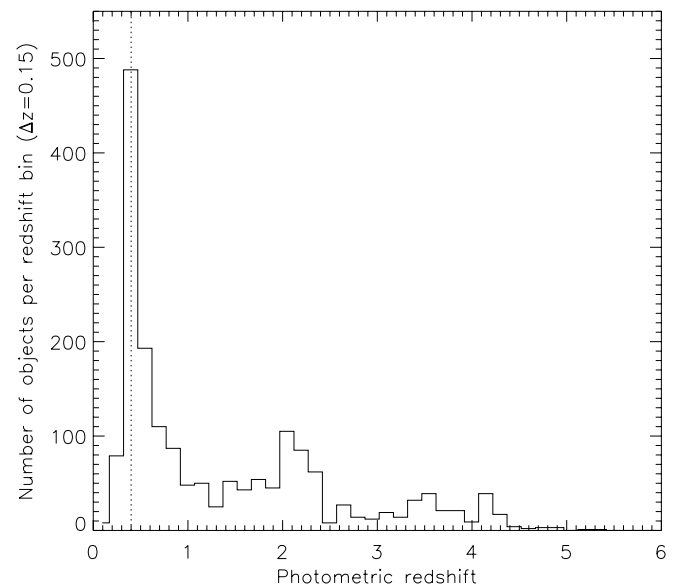


FIG. 4.—Photometric redshift distribution of the  $i_{775} < 27.5$  nonstellar objects in the Cl 0024+17 field. The redshifts are estimated using the six-passband ACS photometry with HDF-N priors. The redshift spike at  $z = 0.4$  (*dashed line*) is clearly visible.

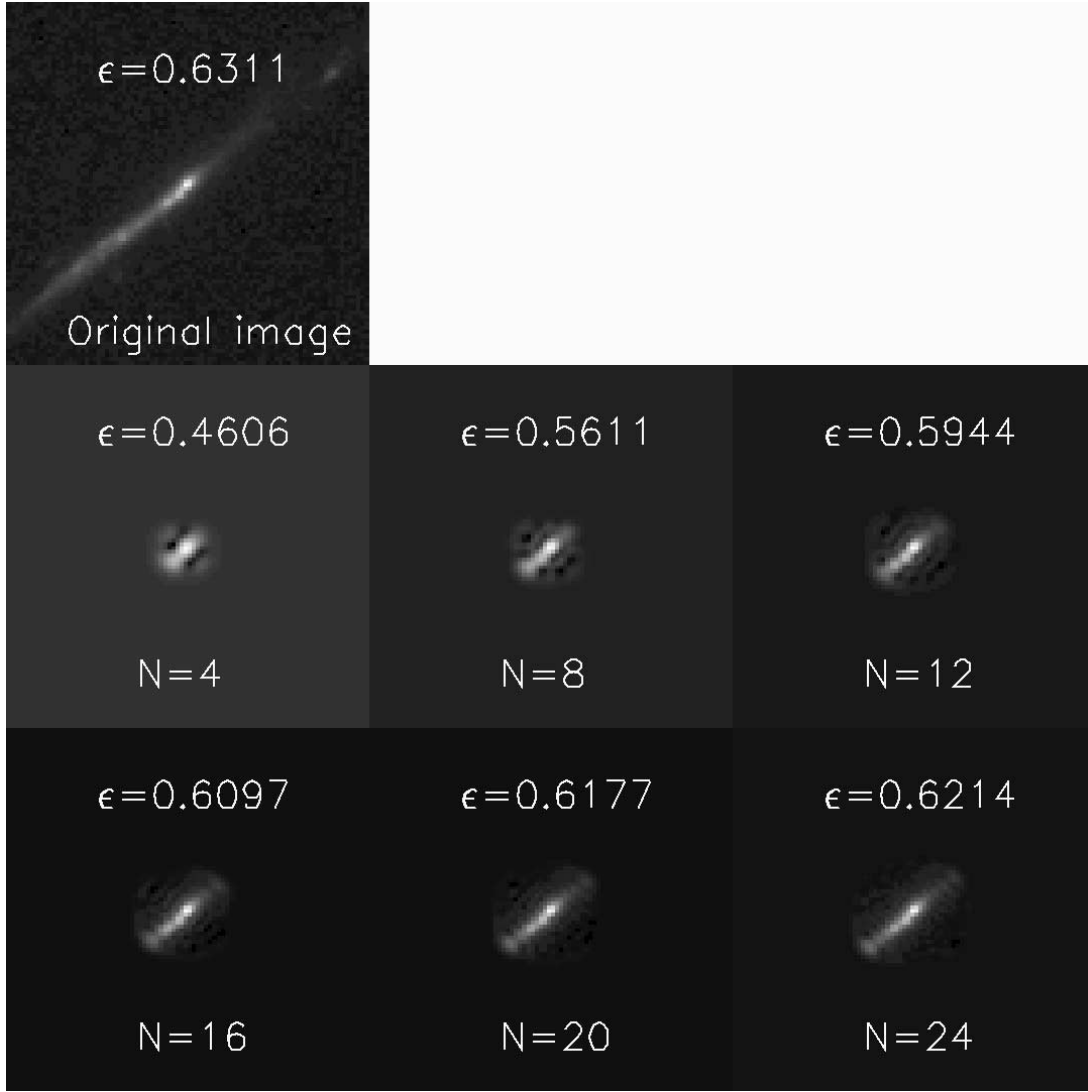


FIG. 5.— Example of aliasing in a shapelet representation. Intensities are on a square root scale. We display the shapelet decomposition and the measured ellipticity  $\epsilon$  of a highly elongated object for different  $N$  (shapelet order). When we measure the ellipticity by directly fitting an elliptical Gaussian function as proposed in the current paper, we obtain  $\epsilon = 0.6311$ . As we increase  $N$ , the recovered ellipticity from the shapelet method approaches this value, yet very slowly.

without reducing the number of usable galaxies substantially. The resulting source catalog contains 1297 objects in the central  $196'' \times 196''$  region of the cluster ( $\sim 120 \text{ arcmin}^{-2}$ ).

### 2.3. Ellipticity Measurements and Point-Spread Function Corrections

As in our previous weak-lensing analyses (Jee et al. 2005a, 2005b, 2006), we use adaptive elliptical Gaussian-weighted moments suggested by Bernstein & Jarvis (2002) to measure source ellipticities. The method has been extensively tested in Bernstein & Jarvis (2002), Hirata & Seljak (2003), Wittman et al. (2003), Park et al. (2004), Margoniner et al. (2005), Jarvis et al. (2003), etc. This elliptical Gaussian weighting reduces the systematic underestimation of the object ellipticities of the Kaiser et al. (1995) method, which uses a circular Gaussian weighting. Previously, the elliptical Gaussian weighting was implemented by adaptively shearing object shapes to match the *circular* Gaussian function in *shapelets* (Refregier 2003; Bernstein & Jarvis 2002).

However, in the current paper, the implementation has been modified and we now determine object shapes by directly fitting the PSF-convolved *elliptical* Gaussian to the pixelized images.

This method is conceptually identical to our previous shapelet approach but provides some important practical merits. The most significant advantage is that the method is better suited for highly elongated objects, which cannot be well represented by shapelets. Shapelets are based on *circular* Gaussian functions and thus introduce nonnegligible aliasing for objects with high ellipticities. One such case is demonstrated in Figure 5. We note that, even for a moderately high order ( $N = 24$ ), the highly elongated shape of the object is not fully recovered and also the decomposition creates some circular ripples around the object center. When we measure the ellipticity by directly fitting an elliptical Gaussian function to the object as proposed in the current study, we obtain  $\epsilon = 0.6311$ , which is slightly higher than the  $N = 24$  shapelet measurement  $\epsilon = 0.6214$ . The conventional Kaiser et al. (1995) method based on a circular Gaussian function yields  $\epsilon = 0.4243$ , substantially lower than the shapelet or the elliptical Gaussian fitting methods. The differences among these three measurements tend to increase for higher ellipticity objects.

In principle, these aliasing features are alleviated when the order of the shapelet decomposition becomes infinite. However,

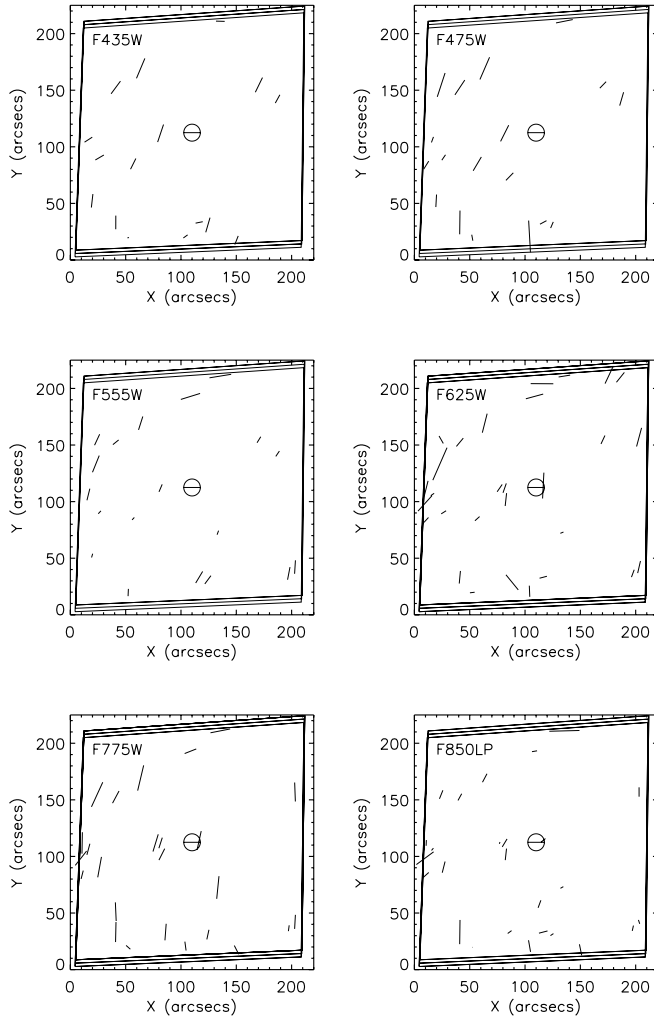


FIG. 6a

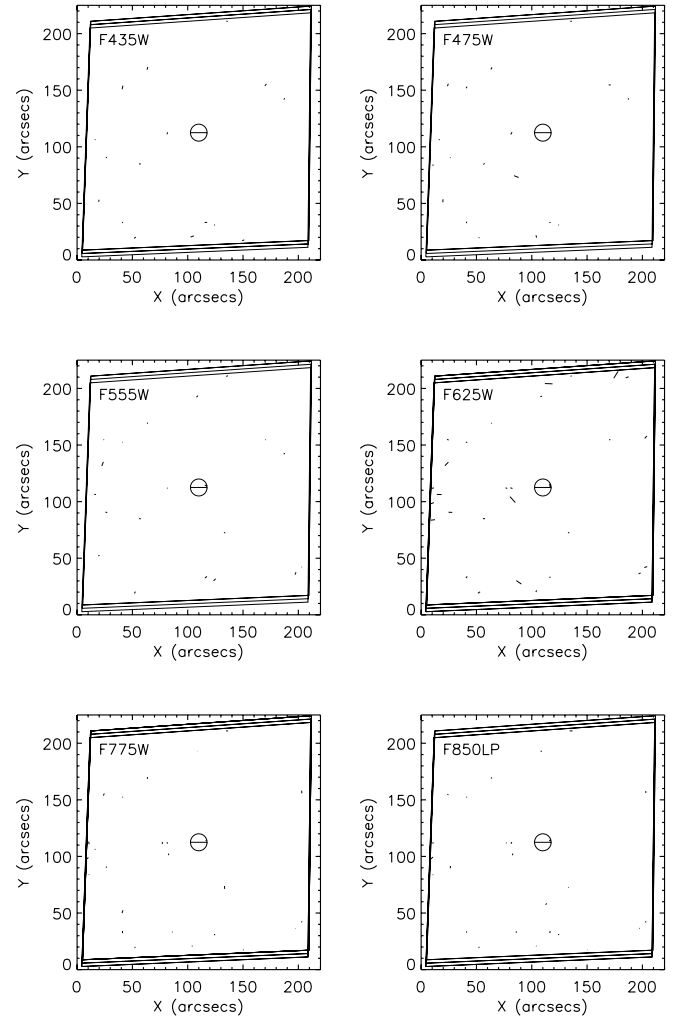


FIG. 6b

FIG. 6.—Observed PSF pattern and correction in the ACS WFC Cl 0024+17 field. The stars are selected from the size vs. magnitude plot. We show the observed ellipticity pattern of the stars (a) before and (b) after the correction. The circled stick in the center illustrates ellipticity of  $\epsilon = 0.05$ .

the convergence is slow and unsatisfactory partly because the pixelization degrades the orthonormality of the basis functions. While this aliasing was not a problem in our previous weak-lensing analyses where not many objects have such high ellipticities, it can create nonnegligible biases in the current lensing study of Cl 0024+17, where the ACS images provide numerous such arc(let)s within the field. In addition, for small objects whose effective radius approaches the size of the PSF, the PSF-convolved elliptical Gaussian fitting is more numerically stable than our previous two-step solution with shapelets (i.e., ellipticity determination after deconvolution).

We create an object ellipticity catalog for each of the six filters and later combine the six catalogs to produce the final ellipticity catalog by weighting each filter's output with its inverse variance; we do not observe any measurable systematic bias in ellipticity measurement between different filters. For each filter, a thumbnail image of an object is created and pixels belonging to other objects, if present, are masked out using the SExtractor segmentation map. The centroid of the object is determined from the detection image (see § 2.1) and is given as initial parameters. We freeze the background value using the SExtractor output, as this gives a more precise sky value than the direct determination within the thumbnail image, especially when bright objects are

nearby. Then, elliptical Gaussian functions are convolved with the ACS PSF before being fitted to the object. Our artificial shear test shows that the object ellipticities measured in this way reliably recover the input shears (see Appendix A).

The PSF of ACS is time- and position-dependent as first noted by Krist (2003). We model the ACS PSF using archival 47 Tuc observations as detailed in Jee et al. (2005a, 2005b, 2006). The position-dependent PSF variation is conveniently described in shapelets with coefficients varying as third-order polynomials of pixel coordinates. Because the global pattern changes depend on the *HST* focus offset, we search the globular cluster images that were observed under a wide range of *HST* focus values for the matching frames whose PSF patterns seem to fit those in the Cl 0024+17 field. We use  $\sim 20$  stars in the Cl 0024+17 field in each filter as the pattern indicators, and the fidelity of the PSF model is verified by checking the roundness of these stars after the Cl 0024+17 image is convolved with rounding kernels created from the model. Figures 6a and 6b show the PSF ellipticities before and after the application of the rounding kernels, respectively. The accuracy of our PSF model for the Cl 0024+17 field, judged from the reduction of the initial PSF anisotropy, is similar to the ones in our previous studies (e.g., Jee et al. 2006), for instance, giving a final mean

ellipticity<sup>9</sup> of  $\epsilon = 0.011 \pm 0.006$  for F435W (and similar values for other filters).

Occasionally, more than one template (star field) is good for the cluster field. Nevertheless, as long as the final mean residual ellipticity of the stars is  $\sim 0.01$  as in the case of the current paper, different templates do not make a difference in our cluster mass reconstruction, where the lensing signal and the statistical errors from intrinsic ellipticity overwhelm the PSF correction residual error. However, we suspect that even this  $\sim 0.01$  level accuracy in PSF correction may be of concern to most cosmic shear studies in the future.

### 3. A NONPARAMETRIC MASS RECONSTRUCTION METHOD COMBINING STRONG- AND WEAK-LENSING SIGNALS

The concept of combining strong- and weak-lensing constraints to derive a cluster mass profile has been previously proposed and applied to observations (e.g., Abdelsalam et al. 1998; Bridle et al. 1998; Seitz et al. 1998; Kneib et al. 2003; Smith et al. 2005; Bradač et al. 2005; Halkola et al. 2006; Cacciato et al. 2006). The approach used in the current study is similar to the method of Seitz et al. (1998), who proposed to use individual galaxy ellipticities *without smoothing* and to reconstruct the mass map through an entropy-regularized maximum likelihood approach. The method also suggests to construct the cluster's scalar potential first and to derive the mass map from this result. This indirect derivation not only avoids the pitfalls of the finite field inversion but also enables an easy incorporation of additional constraints such as strong-lensing features. Seitz et al. (1998) considered a case where magnification information can be directly obtainable from the field. An important modification of the method implemented here is to replace the magnification term in their likelihood function with straightforward multiple-image constraints. A similar modification was also proposed by Bradač et al. (2005). However, they did not utilize the entropy of the mass to regularize the result, and their finite difference scheme for the evaluation of  $\kappa$  is different from ours.

Because there exist a number of excellent review papers on the subject (e.g., Kochanek [2004] for strong lensing and Bartelmann & Schneider [2001] for weak lensing), we summarize only the basic lensing theory and equations in § 3.1 necessary for the description of our implementation (§ 3.2).

#### 3.1. Theoretical Frameworks

Large cosmological distances between the observer, lens, and source galaxies justify the “thin” lens approximation, where the mass distribution of the lens is only two-dimensional. Under this convenient assumption, the deflection  $\alpha$  is handily expressed in terms of the following two-dimensional deflection potential:

$$\psi(\theta) = \frac{1}{\pi} \int d^2\theta' \kappa(\theta') \ln|\theta - \theta'|, \quad (1)$$

$$\alpha = \nabla\psi. \quad (2)$$

In equation (1),  $\kappa$  is the surface mass density in units of the critical surface mass density  $\Sigma_c = c^2 D(z_s)/[4\pi G D(z_l) D(z_l, z_s)]$ , where  $D(z_s)$ ,  $D(z_l)$ , and  $D(z_l, z_s)$  are the angular diameter distance from the observer to the source, from the observer to the lens, and from the lens to the source, respectively. The relation

between  $\kappa$  and  $\psi$  can be more compactly expressed using the gradient  $\nabla$  operator as

$$\kappa = \frac{1}{2} \nabla^2 \psi. \quad (3)$$

The deflection  $\alpha$  (eq. [2]) relates the source position  $\beta$  to the image position  $\theta$  via the lens equation:

$$\beta = \theta - \alpha(\theta). \quad (4)$$

The fact that  $\alpha$  is a function of the image position  $\theta$  implies that a single position in the source plane can be imaged onto multiple locations. In a typical parametric strong-lensing modeling, one uses equations (1)–(4) iteratively to construct the mass model  $\kappa(\theta)$  that correctly inverts all the sets of known multiple-image positions to single-source positions. In a weak-lensing regime where the surface mass density is low (i.e.,  $\kappa < 1$ ), the system does not produce multiple images. However, one can still detect coherent shape distortions of source galaxies. The Jacobian matrix describing the distortion is obtained from the above lens equation (eq. [4]):

$$\mathbf{A} \equiv \frac{\partial \beta}{\partial \theta} = \begin{pmatrix} 1 - \psi_{11} & -\psi_{12} \\ -\psi_{12} & 1 - \psi_{22} \end{pmatrix} = \begin{pmatrix} 1 - \kappa - \gamma_1 & -\gamma_2 \\ -\gamma_2 & 1 - \kappa + \gamma_1 \end{pmatrix}, \quad (5)$$

where the subscripts on  $\psi_{i(j)}$  denote partial differentiation with respect to  $\theta_{i(j)}$ , and the shears  $\gamma_1$  and  $\gamma_2$  are

$$\gamma_1 = \frac{1}{2} (\psi_{11} - \psi_{22}) \quad (6)$$

and

$$\gamma_2 = \psi_{12} = \psi_{21}, \quad (7)$$

respectively. It is convenient to express the shears  $\gamma_{1(2)}$  in complex notation:  $\gamma = \gamma_1 + i\gamma_2$ . The Jacobian matrix (eq. [5]) transforms a circle into an ellipse with an ellipticity  $\hat{g}$ :

$$\hat{g} = \begin{cases} g, & |g| < 1, \\ \frac{1}{g^*}, & |g| > 1, \end{cases} \quad (8)$$

where  $g$  is the reduced shear  $g = \gamma/(1 - \kappa)$  (complex notation) and  $g^*$  denotes the complex conjugate of  $g$ . Note that the absolute value of  $\hat{g}$  above yields an ellipticity defined in the current paper.

Assuming that the intrinsic ellipticity distribution is isotropic, the mean ellipticity of galaxies under the reduced shear  $g$  is simply  $\hat{g}$  following the rule in equation (8). However, many practical ellipticity measurements yield values systematically different from (in general lower than)  $\hat{g}$ . For example, the conventional Kaiser et al. (1995) method uses a circular Gaussian weighting in the measurement of the object second moments, and this choice of weighting circularizes object shapes, resulting in the underestimation of the local shear (e.g.,  $\sim 20\%$  lower at  $\hat{g} \sim 0.4$ ). Our shear estimation utilizing an elliptical Gaussian as a weighting scheme reduces such a systematic underestimation substantially as shown in Appendix A. Nevertheless, our numerical simulation demonstrates that in a highly nonlinear regime ( $\hat{g} > 0.4$ ) our ellipticity measurement still slightly

<sup>9</sup> Note that in our previous papers, an ellipticity of a star was defined as  $(a^2 - b^2)/(a^2 + b^2)$ , which is approximately a factor of 2 larger than the current definition  $(a - b)/(a + b)$  for small values.



underestimates the input shear partly because the galaxies bend and become arclets. Potentially, this second-order lensing effect (termed “flexion” in Goldberg & Natarajan 2002) can be utilized in the improvement of the local shear estimation (for the suggestion of using shapelets for the flexion measurement see also Massey et al. 2006). In the current investigation, we determine the correction factors by simulation and use them in our mass reconstruction.

So far, we have only considered a single source plane at a fixed redshift. In practice, source galaxies span a wide range of redshifts, and the above equations must be scaled accordingly. We choose  $z_f = 3$  as the fiducial redshift and express the deflection potential (and the derived quantities) of the cluster with respect to the source plane at  $z_f$ . The translation of these physical values from  $z_f$  to a given redshift  $z$  is straightforward. Using the “cosmological weight” function

$$W(z, z_f) = \frac{D(z_f)D(z_l, z)}{D(z_l, z_f)D(z)}, \quad (9)$$

the surface mass density  $\kappa$ , shear  $\gamma$ , and deflection  $\alpha$  are scaled as

$$\kappa(z) = W(z, z_f)\kappa(z_f), \quad (10)$$

$$\gamma(z) = W(z, z_f)\gamma(z_f), \quad (11)$$

and

$$\alpha(z) = W(z, z_f)\alpha(z_f), \quad (12)$$

respectively. In addition, the reduced shear at a redshift of  $z$  is now given as

$$g(z) = \frac{W(z, z_f)\gamma(z_f)}{1 - W(z, z_f)\kappa(z_f)}. \quad (13)$$

The expected mean ellipticity at a redshift of  $z$  is then obtained by the rule in equation (8).

### 3.2. Implementation

We seek to construct a two-dimensional cluster deflection potential that correctly predicts the observed locations of the multiple images and the ellipticity distribution of background galaxies in the ACS observations. Because an observed lensing signal (i.e., shears and deflection) relates to a cluster mass only via a convolution, a direct modeling of the mass distribution within a finite field is subject to biases (masses outside the field can affect the shears inside). Although one can attempt to alleviate this problem by extending the field by a few factors, the scheme increases the number of unknown parameters substantially, causing the minimization procedure to become prohibitively cumbersome. On the other hand, the deflection potential can be locally converted to shears, deflection field, and mass density via equations (2), (3), (6), and (7). Therefore, we favor the direct estimation of the cluster lensing potential as also advocated by many other authors (e.g., Bartelmann et al. 1996; Seitz et al. 1998; Bradač et al. 2005).

We set up a  $52 \times 52$  potential grid over the central  $210'' \times 210''$  region of CI 0024+17. At the inner  $50 \times 50$  ( $196'' \times 196''$ ) lattice points the shear  $\gamma$ , deflection field  $\alpha$ , and mass density  $\kappa$  are calculated by the central finite difference method. Note that we use the five nearest points as in Seitz et al. (1998) to evaluate

$\kappa$ , whereas Bradač et al. (2005) used the four additional diagonal points (a total of nine).

Then, these values at lattice points are bicubic interpolated to estimate the lensing observables at each galaxy location. We find that the bicubic interpolation provides not only a smoother result but also smaller  $\chi^2$  values than the bilinear interpolation although the evaluation is computationally much more expensive. Particularly, we notice that the bicubic interpolation substantially outperforms the bilinear interpolation in the deprojection of the multiply lensed objects.

When evaluating  $\gamma_2$  at the four corners of the  $50 \times 50$  grid, we use the finite difference scheme of equation (25.3.27) in Abramowitz & Stegun (1984), following the suggestion of Seitz et al. (1998). This prevents the four corners of the  $52 \times 52$  potential grid from being used in the minimization below.

We now desire to find a set of parameters describing the cluster potential by minimizing the following function:

$$f = \frac{1}{2}\chi_\mu^2 + \frac{1}{2}L_\epsilon + R, \quad (14)$$

where  $\chi_\mu^2$  is the dispersion of multiple images in the source plane,  $L_\epsilon$  is the log-likelihood function for the shear, and  $R$  is the regularization term that is required to prevent the minimization procedure from overfitting the data. The factor  $\frac{1}{2}$  in the first and second term is included to ensure that the posterior probability distribution is proportional to  $\exp[-(f - f_m)]$  (i.e., without any additional factor in front of  $f$ ), where  $f_m$  is the value of equation (14) at the global minimum.

We define  $\chi_\mu^2$  for a single source at a redshift  $z$  with  $M$  multiple images and  $N$  knots as

$$\chi_\mu^2 = \sum_{m=1}^M \sum_{n=1}^N \frac{[\theta_{m,n} - W(z, z_f)\alpha(\theta_{m,n}) - \beta_n]^2}{\sigma_{m,n}^2}, \quad (15)$$

$$\beta_n = \frac{1}{M} \sum_{m=1}^M [\theta_{m,n} - W(z, z_f)\alpha(\theta_{m,n})], \quad (16)$$

where  $\theta_{m,n}$  and  $W(z, z_f)\alpha(\theta_{m,n})$  are the coordinate of the  $n$ th knot of the  $m$ th multiple image and the scaled deflection at its redshift  $z$ , respectively.

The choice of  $\sigma_{m,n}$  is important. Using a fixed value throughout the minimization biases the model toward high magnification because the numerator of equation (15) decreases as the magnification increases regardless of the goodness of the agreement of individual knots. This often leads to incorrectly small  $\chi_\mu^2$  values (thus also unreasonably small error estimates for the fitting parameters). One possible solution is to utilize the magnification tensor  $M$  to scale the error according to the magnification. However, this scheme becomes numerically very unstable and  $\chi_\mu^2$  diverges if any of the multiple images are close to critical curves. In the current implementation, we developed a novel, simple scheme, which does not bias the model toward high magnification but without the use of the magnification tensor. We normalized the coordinates of the knots of the multiple images in the source plane in such a way that they always range between zero and one. These normalized coordinates change as we iterate. Then, a fixed value of the uncertainty becomes a fractional uncertainty and no longer biases the model toward high magnification. Nevertheless, there is one concern about this normalization. A solution where the source positions have a couple of outliers (i.e., setting the 0–1 scaling) plus a cluster of points with small scatter can also yield low  $\chi_\mu^2$  values. However, this configuration is highly disfavored in practice for the following two reasons. First,



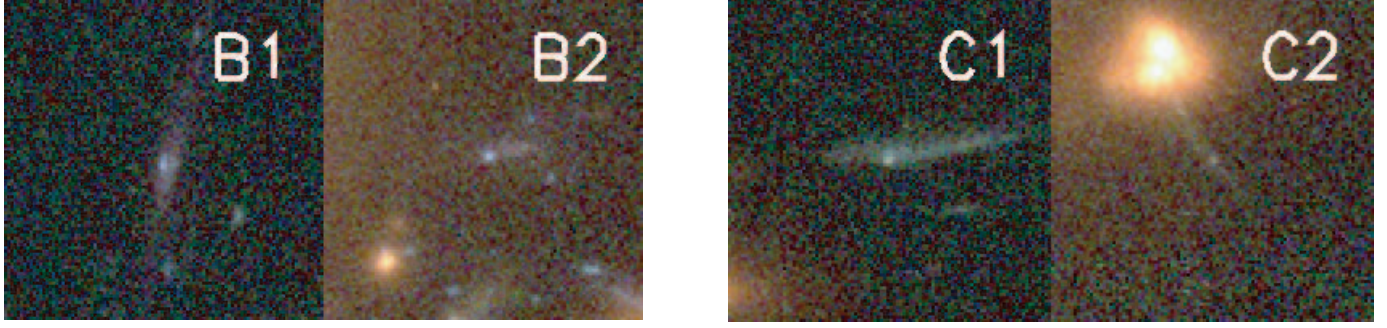


FIG. 7.—Two additional multiple-system candidates used as strong-lensing constraints. The B1–B2 system is originally identified by Broadhurst et al. (2000) with WFPC2 observations. The photometric redshift of the system is  $\bar{z}_{\text{phot}} = 1.27$ . Our initial mass model based on this B1–B2 system along with the A1–A5 system predicts that the C1–C2 images with  $\bar{z}_{\text{phot}} = 2.84$  are also multiply lensed.

the weak-lensing signals tend to keep the solution away from the mass model that predicts such an unusual source configuration. Second, once all the source positions are “locked” closely, further iterations do not produce such outliers because a source position “drifting” away from the rest of the source locations increases the above  $\chi_\mu$  steeply. The exact value of  $\sigma_{m,n}$  is not critical but should not be set too small as the model is limited by the finite resolution of the grid and interpolation errors.

It is appropriate to point out here that the above source plane minimization can be potentially replaced with an image plane minimization (Kochanek 2004), where the predicted source positions are compared with their observed positions in the image plane. This scheme would obviate the need to rescale the  $\sigma_{m,n}$  values as required in the current source plane minimization. Furthermore, the minimization would disfavor the model that predicts any unobserved image because it can now penalize the resulting  $\chi_\mu^2$  values. Unfortunately, the image plane minimization is computationally much more expensive, requiring a non-trivial image plane search. Because our system already involves the time-consuming numerical estimation of the function derivatives (see below), this image plane minimization is highly unfeasible if not impossible in the current approach. However, we emphasize that the above source plane minimization with re-normalization of the source plane coordinates prevents the model from being biased toward high magnification. The only remaining concern is occasional prediction of unobserved multiple images. Nevertheless, the presence of these unobserved multiple images should not discredit the model because, as discussed in § 4.4, the converged potential can be always modified manually to remove those spurious objects by making some negligible changes to the model.

We used the well-known five multiple images from the single source at  $z = 1.675$  and two additional multiple-system candidates in the evaluation of equation (15). The locations of these two new systems in the cluster field are denoted as B1–B2 and C1–C2 in Figure 1, and their cutout images are shown in Figure 7. In theory, the total number of multiple images in an extended lens is always odd as long as the inner mass profile is shallower than the singular isothermal (i.e.,  $\propto r^{-2}$ ) profile. Nevertheless, it is well known that many observed lens images seem to have two or four images because the third or fifth image is usually either much fainter or obscured by bright galaxies. In the current cluster C1 0024+17 we also have not yet found any convincing third image candidate for the B1–B2 and C1–C2 systems. The B1–B2 system is originally identified by Broadhurst et al. (2000) with WFPC2 observations. The photometric redshift of the system is  $\bar{z}_{\text{phot}} \simeq 1.3$ . Our initial mass model based on this B1–B2

system along with the A1–A5 system predicts that the C1–C2 images with  $\bar{z}_{\text{phot}} \simeq 2.8$  are also multiply lensed. We impose relatively loose constraints to the convergence of these two systems, considering the typical, large uncertainty ( $\delta z \sim 0.1$ ) of the photometric redshift estimation and the lack of morphological features of these systems. We set  $\sigma_{m,n}$  to 0.03 for A1–A5 and to 0.3 for B1–B2 and C1–C2; an order of magnitude larger  $\sigma_{m,n}$  values are used for B1–B2 and C1–C2. These values are empirically determined in our attempt to make the above  $\chi_\mu^2$  per degree of freedom become close to unity.

The individual galaxies in the A1–A5 multiple system are well resolved, and we choose 10 bright knots for each source as inputs to equation (16) ( $10 \times 5 \times 2 = 100$  constraints). Although Tyson et al. (1998) claim that they can characterize each source with 58 smooth disks (four parameters for each disk) in their modeling, our experiments demonstrate that increasing the number of constraining features further does not improve the model; because the deflection field varies very smoothly, excessively additional constraints provide only redundant information. The B1–B2 and C1–C2 systems possess relatively unclear morphology, and thus we characterize each source with only four positions ( $4 \times 4 \times 2 = 32$  constraints).

The log-likelihood function  $L_\epsilon$  can be derived from the assumption that the ellipticity distribution for the presence of the reduced shear  $g$  is a Gaussian:

$$p_\epsilon(\epsilon|g) \propto \frac{1}{\pi\sigma_\epsilon^2(\hat{g})} e^{-|\epsilon - \hat{g}|^2/\sigma_\epsilon^2(\hat{g})}. \quad (17)$$

Although we know that the exact shape of the lensed ellipticity distribution is not Gaussian, equation (17) is a convenient approximation, which represents the first and second moments of the lensed ellipticities (Geiger & Schneider 1999).

Then, the log-likelihood function for  $K$  background galaxies is given as

$$L_\epsilon = \sum_{k=1}^K \left[ \frac{|\epsilon_k - \hat{g}|^2}{\sigma_k^2(\hat{g})} + \ln \sigma_k^2(\hat{g}) \right], \quad (18)$$

where  $\sigma_k(\hat{g})$  is the ellipticity dispersion for the  $k$ th galaxy under the influence of the shear  $g$  and can be approximated by adding the intrinsic ellipticity dispersion and the measurement error in quadrature:  $\sigma_k^2(\hat{g}) = \sigma_\epsilon^2(\hat{g}) + \sigma_{k,\text{err}}^2$ . The ellipticity dispersion for a given  $\hat{g}$  is often assumed to follow the simple analytic form

$$\sigma_\epsilon(\hat{g}) = \sigma_\epsilon(0)(1 - \hat{g}^2), \quad (19)$$

where  $\sigma_\epsilon(0)$  is the intrinsic ellipticity dispersion of the source population in the absence of gravitational lensing. From our artificial shear test, we find that equation (19) with  $\sigma_\epsilon(0) \sim 0.3$  is a good approximation over a wide range of  $\hat{g}$ . Nevertheless, it slightly underestimates the true dispersion at low  $\hat{g}$  and overestimates the value at high  $\hat{g}$ . Therefore, we attempt to obtain a better analytic expression and find that the relation

$$\sigma_\epsilon(\hat{g}) = 0.31(1 - \hat{g}^2)^{1.11} \quad (20)$$

provides a better fit to the simulation result (see Appendix B).

Finally, we need to define the regularization  $R$ , which governs the overall smoothness of the mass reconstruction. The need for this regularization  $R$  is obvious when we compare the number of free parameters 2697 (see below) with the number of the constraints 2726 ( $1297 \times 2 = 2594$  from the ellipticities and 132 from the multiple images). Without the regularization, the minimization will overfit the data unless the number of constraints is significantly larger than the number of parameters. We adopt the following maximum entropy regularization (Press et al. 1992) implemented by Seitz et al. (1998):

$$R = \eta \sum_{p,q} \hat{\kappa}_{p,q} \ln \left( \frac{\hat{\kappa}_{p,q}}{b_{p,q}} \right), \quad (21)$$

where  $\hat{\kappa}_{p,q}$  and  $b_{p,q}$  are the surface mass density and prior at the grid point  $(p, q)$ , respectively, normalized in such a way that the summation over the entire grid becomes unity. The maximum entropy method (MEM) leads to a mass reconstruction as smooth as possible while preserving details that the data constrain. The parameter  $\eta$  is to control the smoothness of the resulting mass map and needs to be adjusted in such a way that  $\chi^2$  per degree of freedom remains close to unity.

As suggested by Seitz et al. (1998), one can use the result of the direct mass reconstruction as an initial prior and update it at the beginning of the next minimization step with the smoothed version of the previous mass map. However, the choice of the initial prior does not determine the final result, and one can start the minimization with a flat prior to reach the virtually identical final result, but of course with many more iterations. As mentioned above, the four corner points of the  $52 \times 52$  grid do not enter the minimization. In addition, because the zero point of the deflection potential and the translation of the source plane are arbitrary, we need to fix three additional grid points. Therefore, the number of free parameters is  $(50 + 2) \times (50 + 2) - 7 = 2697$ .

We choose the Davidon-Fletcher-Powell (DFP) algorithm (Press et al. 1992) as our main optimization scheme to minimize the target function (eq. [14]). The DFP algorithm constructs an inverse Hessian matrix iteratively and uses it along with the partial derivatives of the function to determine the next iteration point  $\psi$ :

$$\psi - \psi_i = -\mathbf{A}^{-1} \cdot \nabla f(\psi_i). \quad (22)$$

The complexity of our target function (i.e., the use of bicubic interpolation, maximum entropy regularization, etc.) makes it nontrivial, if not impossible, to write the derivatives  $\partial f / \partial \psi_k$  in linear terms of  $\psi_k$ . Therefore, we feed numerically calculated derivatives to the IDL implementation of the algorithm (DFPMIN). Although the above algorithm is efficient, we find that the minimization occasionally gets stuck in local minima. Hence, we complement the minimization procedure with the gradient-free Direction-Set method (Press et al. 1992). In general, this min-

imization scheme, which does not require explicit evaluation of the gradients of the target function, converges slower than the DFP method above or other gradient-based techniques (e.g., conjugate gradient method). However, we observe that this Direction-Set method more effectively resolves the local minimum. Consequently, we restart the minimization with this second algorithm whenever the DFP minimization converges to local minima. Although it is in general extremely difficult to reach a unique set of parameters for a large system in a strictly mathematical sense, we are convinced that our final set of parameters are very close to the *true* global minimum. We examine the quasi uniqueness of our solution in two ways. First, we repeat the minimization with different choices of initial conditions (and priors) and verify that they all lead to *virtually* identical results. Second, we perturb the converged set of parameters by adding small random numbers and execute the minimization with this new set of parameters. No significant drifts from the original set of parameters are observed.

### 3.3. Uncertainties of the Mass Reconstruction

The proper interpretation of the features in the mass reconstruction necessitates our understanding of the noise properties. In general, the complex relation between lensing observables and the derived mass map makes the noise estimation nontrivial. In the current study, we choose to estimate the uncertainties utilizing the Hessian matrix of the target function  $f$  (eq. [14]) at the location of the minimum  $\hat{\psi}$ . When  $\psi$  is sufficiently close to the location of the function minimum  $\hat{\psi}$ , the target function  $f$  can be approximated by a quadratic form:

$$f(\psi) \simeq f(\hat{\psi}) + (\psi - \hat{\psi}) \cdot \nabla f(\hat{\psi}) + \frac{1}{2} (\psi - \hat{\psi}) \cdot \mathbf{A} \cdot (\psi - \hat{\psi}), \quad (23)$$

where the first-order term vanishes because  $\nabla f = 0$  at  $\hat{\psi}$ . By exponentiating the above equation, we get the posterior distribution:

$$P(\psi) \propto \exp \left\{ -[f(\psi) - f(\hat{\psi})] \right\} \propto \exp \left[ -\frac{1}{2} (\psi - \hat{\psi}) \cdot \mathbf{A} \cdot (\psi - \hat{\psi}) \right]. \quad (24)$$

That is, the posterior distribution  $P(\psi)$  becomes Gaussian in the neighborhood of  $\hat{\psi}$  with a covariance matrix being the inverse of the Hessian  $\mathbf{A}^{-1}$ . Bridle et al. (1998) show that this Gaussian approximation agrees with the result from their Monte Carlo experiments. Of course, because we estimate the deflection potential  $\psi$  (not the convergence  $\kappa$  directly) in our study, it is necessary to propagate the errors, accordingly.

## 4. GRAVITATIONAL LENSING ANALYSES

### 4.1. Mass Reconstruction and Discovery of an $r \simeq 0.4$ Mpc Ringlike Dark Matter Structure

Our mass reconstruction of CI 0024+17 is presented in Figure 8. Figure 8a shows the  $50 \times 50$  mass map derived from the converged  $52 \times 52$  deflection potential. The corresponding rms map (Fig. 8b) is derived from the Gaussian approximation (§ 3.3). We note that the rms map yields a mean uncertainty of  $\bar{\kappa} \sim 0.02$ , giving higher values at the field boundary and lower values for the region constrained by the strong-lensing data. Also displayed is the bicubic interpolated version (Fig. 8c) with a stretched gray-scale table to emphasize the low-contrast feature. This map was reproduced with a slightly larger regularization constraint (the final ellipticity  $\chi^2$  per galaxy is  $\sim 1.3$ ).

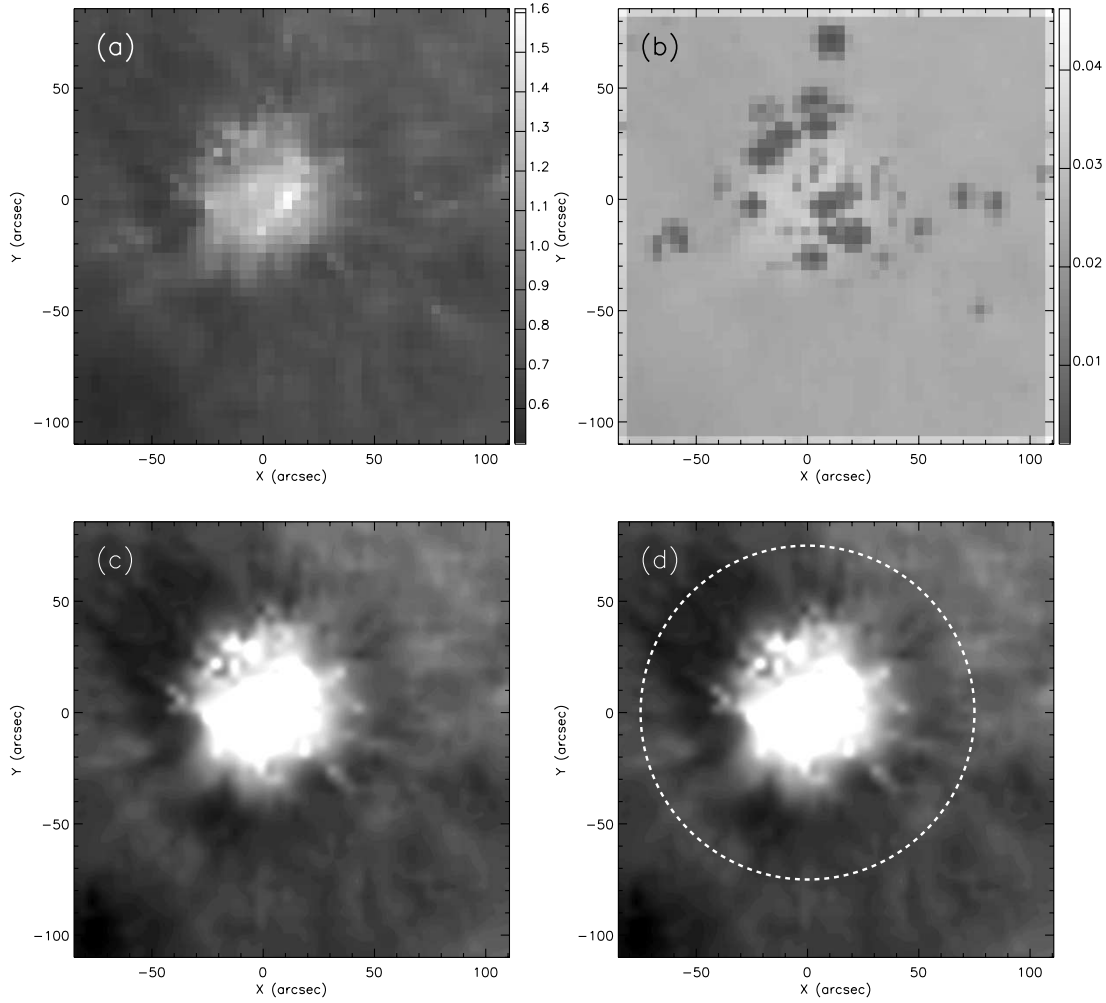


FIG. 8.—Mass reconstruction of Cl 0024+17. (a) The  $50 \times 50$  mass map derived from the converged  $52 \times 52$  deflection potential. (b) Uncertainty of the mass reconstruction derived from the Gaussian approximation (§ 3.3). (c) Same as (a), but we reproduced the map with a slightly larger regularization constraint. The bicubic interpolated result is displayed with a stretched gray-scale table to emphasize the low-density feature. (d) Same as (c), with a dashed circle overlaid at  $r = 75''$  to trace the ringlike substructure observed at that radius. We choose the origin to be the geometric center of the ringlike structure. [See the electronic edition of the *Journal* for a color version of this figure.]

The mass map reveals the striking substructure of Cl 0024+17, characterized by the soft, high-density core at  $r \lesssim 50''$  and the moderately overdense, ringlike substructure at  $r \sim 75''$  (see also Fig. 8d). The ringlike substructure is strongly constrained by the weak-lensing signals at  $r \gtrsim 50''$  and appears even when the mass reconstruction is performed *without* the strong-lensing data. The feature can be also clearly identified in the radial density profile (§ 4.2) and in the tangential shear profile (§ 4.3). In the absence of the “ring,” the mean mass density in the annulus ( $r = 65''$ – $85''$ ) is  $\kappa \sim 0.65$ . With respect to this “background” density, the feature is significant at  $\gtrsim 5 \sigma$  levels. Because of the finite number and the nonuniform distribution of background galaxies, the ringlike feature is lumpy on a small scale. We also note that there is somewhat large-scale azimuthal variation on the structure, which is discussed in the context of the origin of the feature in § 5.1.

The mass peak is in good spatial agreement with the giant elliptical galaxies in the cluster center and is elongated in the direction defined by the three collinear galaxies (see Figs. 9a and 9b). Moreover, this mass peak coincides with the X-ray peak first revealed by *Chandra*, which also appears to possess an elongation in the same direction (Figs. 9c and 9d). By a careful comparison, however, we note that the X-ray centroid is offset to the

northeast by  $\sim 10''$  and is close to the galaxy 380 ( $\alpha_{J2000.0} \simeq 00^h 26^m 36.03^s$ ,  $\delta_{J2000.0} \simeq 17^\circ 09' 45.9''$ ), whereas the mass centroid is near the galaxy 374 ( $\alpha_{J2000.0} \simeq 00^h 26^m 35.69^s$ ,  $\delta_{J2000.0} \simeq 17^\circ 09' 43.12''$ ); in referring to the galaxies we use the object IDs defined in the catalog of Czoske et al. (2002).

Broadhurst et al. (2000) modeled the cluster strong-lensing mass by placing eight *circular* Navarro-Frenk-White (NFW) halos on top of bright elliptical galaxies. Their mass map also shows that the three collinear galaxies mentioned above define the mass peak. Comerford et al. (2006) were also able to reproduce the five multiple images, yet only including those three elliptical galaxies, modeling them as three *elliptical* NFW halos. Because the presence of the fifth image (i.e., denoted A5 in Fig. 1) strongly constrains the location of the mass peak, it is not unexpected to observe the good agreement in the location of the mass peak among the different lensing studies.

#### 4.2. Radial Mass Profile

From the two-dimensional mass map in Figure 8, we can infer that the mass distribution is nearly axisymmetric and also the projected density does not decrease in a monotonic manner as a function of radius. The soft core is surrounded by a low-density annulus at  $r \sim 50''$  and then by moderately high density ringlike

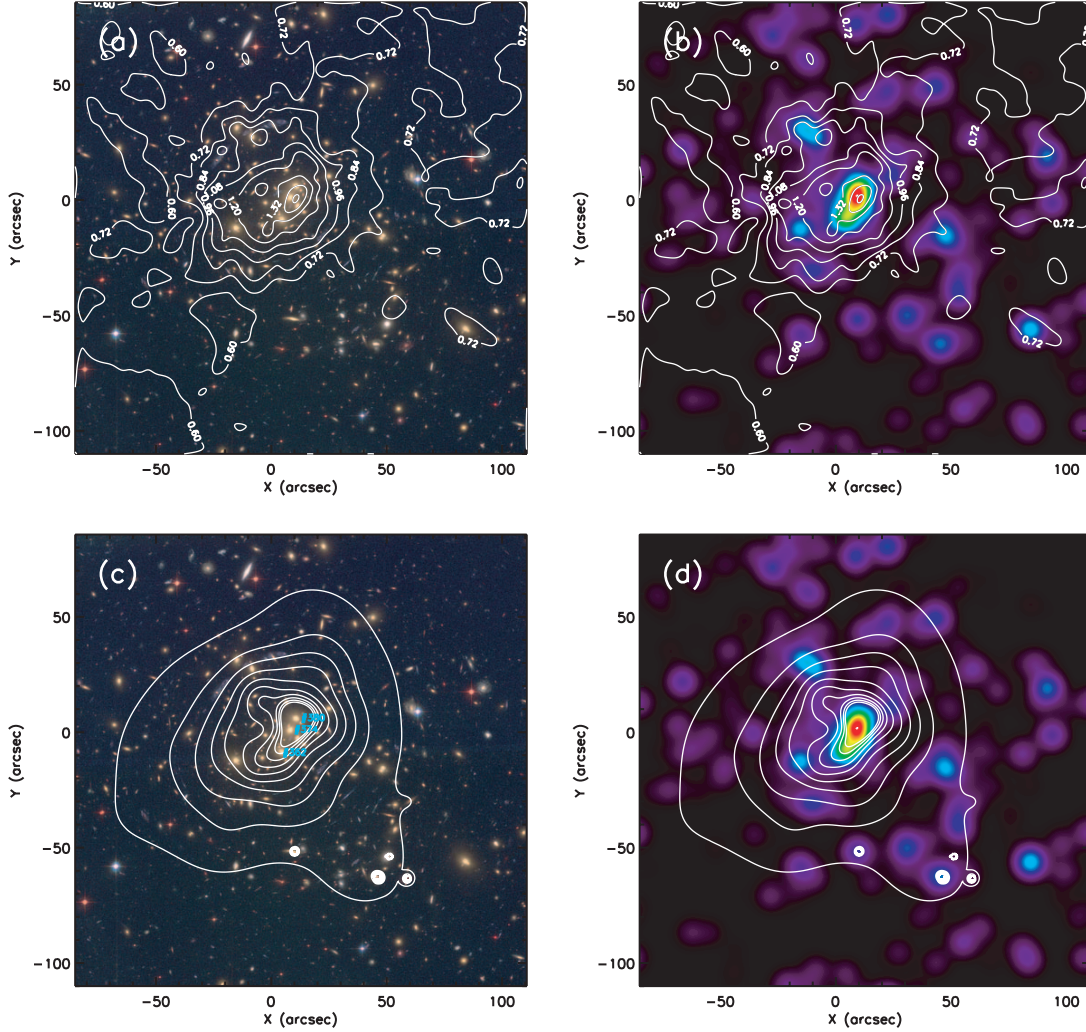


FIG. 9.— C1 0024+17 mass and X-ray overlaid on cluster lights. (a) Mass contours overlaid on the ACS color composite. (b) Mass contours on the smoothed (FWHM  $\sim 10''$ ) cluster light ( $r_{625}$ ) distribution. (c) *Chandra* X-ray contours on the ACS color composite. The X-ray image was exposure corrected and adaptively smoothed (Ebeling et al. 2006) with a minimum significance of  $3\sigma$ . (d) Same as (c), but the background is replaced with the smoothed light distribution.

structure at  $r \sim 75''$ . Here we examine the radial mass density profile of the C1 0024+17 in detail. We choose the geometric center of the ringlike structure ( $\alpha_{J2000.0} \simeq 00^h26^m35.92^s$ ,  $\delta_{J2000.0} \simeq 17^\circ09'35.5''$ ) as the cluster center to calculate the azimuthally averaged density profile (Fig. 10). The core and ring revealed in our previous two-dimensional mass reconstruction are also visible in this radial mass density plot. The projected density of the cluster flattens outside the core and creates the “bump” at  $r \sim 75''$ . The shape of the mass profile in this region is strongly constrained by the weak-lensing signals; the feature appears as a “trough” in the tangential shear profile (see § 4.3). The dotted lines represent the  $1\sigma$  deviation of the azimuthal mean, which reflect not only the noise level but also the intrinsic azimuthal variation. Because of the off-centered mass peak, the azimuthal deviation is large at small radii ( $r \lesssim 20''$ ). In § 4.1 we estimated the significance of the ringlike structure to be at least  $5\sigma$  from the two-dimensional mass profile and the derived rms map. In this one-dimensional profile, the significance of the bump in the  $r = 60''\text{--}85''$  region with respect to the azimuthal mean ( $\bar{\kappa} \simeq 0.65$ ) at the trough ( $r \sim 55''$ ) or the “tail” ( $r \sim 90''$ ) is  $\sim 8\sigma$ .

The overall shape of this radial density profile looks more striking when compared to the results of the previous studies (Fig. 11). We transformed the results of Tyson et al. (1998)

(dotted line), Broadhurst et al. (2000) (dashed line), and Ota et al. (2004) (dot-dashed line) using the current cosmological parameters. A significant difference among the models is undeniable. As already indicated by Ota et al. (2004), the X-ray mass is far less than the other three lensing results; a more recent X-ray analysis with *XMM-Newton* (Zhang et al. 2005; omitted here) yields even slightly lower values. The low core densities ( $\kappa < 1$ ) predicted by these X-ray analyses violate the fundamental condition of the strong lensing, which requires a projected mass density greater than unity in the cluster core.

The result of Tyson et al. (1998) gives the highest core density at  $r \lesssim 15''$  but the lowest density at large radii  $r \gtrsim 20''$ . Because the locations of the critical curves at a fixed redshift are invariant under the transformation  $\kappa \rightarrow \lambda\kappa + (1 - \lambda)$ , a strong-lensing modeling based on single-redshift multiple images is subject to this mass-sheet degeneracy. Therefore, the two lensing mass profiles of Tyson et al. (1998) and Broadhurst et al. (2000) inside the Einstein radius will roughly overlap each other under the above transformation with a proper choice of  $\lambda$ . However, this degeneracy is lifted in our result with the help of the two added source planes at  $z = 1.3$  and  $2.8$ . Moreover, the weak-lensing data extended to the critical regime provide additional constraints in resolving the degeneracy because the arc(let)



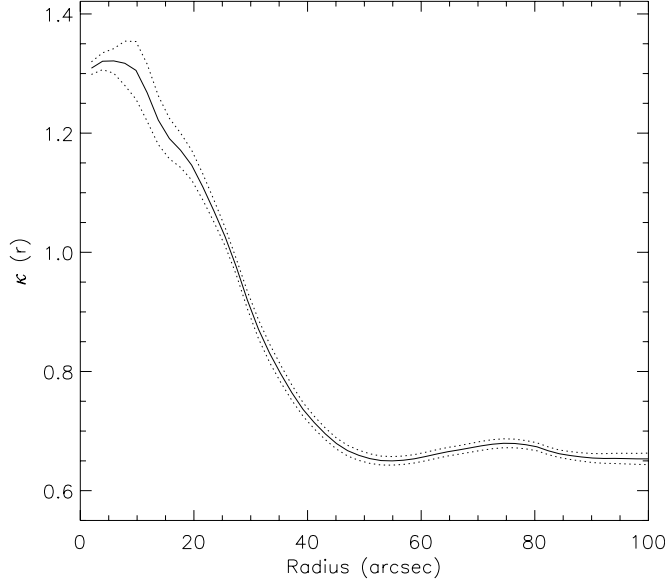


FIG. 10.—Radial mass density profile of Cl 0024+17. The mass density (solid line) is given in units of critical density  $\Sigma_c$  at a fiducial redshift of  $z_f = 3$ . The dotted lines represent the  $1\sigma$  deviation of the azimuthal average. It is clear that the radial mass profile of the cluster is peculiar and does not resemble any conventional analytic profile. At  $r \lesssim 50''$ ,  $\kappa$  decreases for increasing  $r$ . Outside the core ( $r \gtrsim 50''$ ),  $\kappa$  rises and creates a bump at  $r \sim 75''$ .

whose shears approach  $g \sim 1$  inform us of the redshift-dependent, critical curve locations.

The mass profile of Broadhurst et al. (2000) is, nevertheless, somewhat similar to our mass profile at  $r \lesssim 30''$ , but the difference is observed at larger radii. Our mass profile outside the

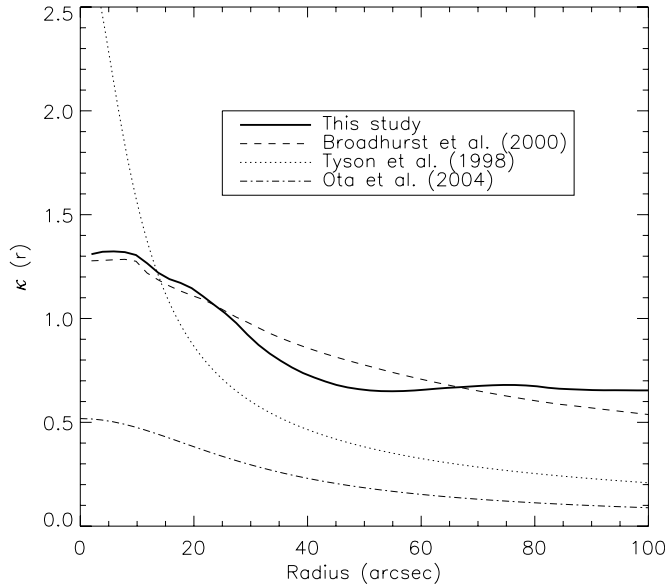


FIG. 11.—Density profiles of Cl 0024+17 from different studies. The overall shape of our radial density profile (solid line) looks more striking when compared to the results of the previous studies. We transformed the results of Tyson et al. (1998) (dotted line), Broadhurst et al. (2000) (dashed line), and Ota et al. (2004) (dot-dashed line) using the current cosmological parameters. Note that Tyson et al. (1998) and Broadhurst et al. (2000) derived the mass density using strong lensing while Ota et al. (2004) used *Chandra* X-ray observations. As already indicated by Ota et al. (2004), the X-ray mass is far less than the other three lensing results; a more recent X-ray analysis with *XMM-Newton* (Zhang et al. 2005; omitted here) yields even slightly lower values. The low core densities ( $\kappa < 1$ ) predicted by these X-ray analyses violate the fundamental condition of the strong lensing, which requires a projected mass density greater than unity.

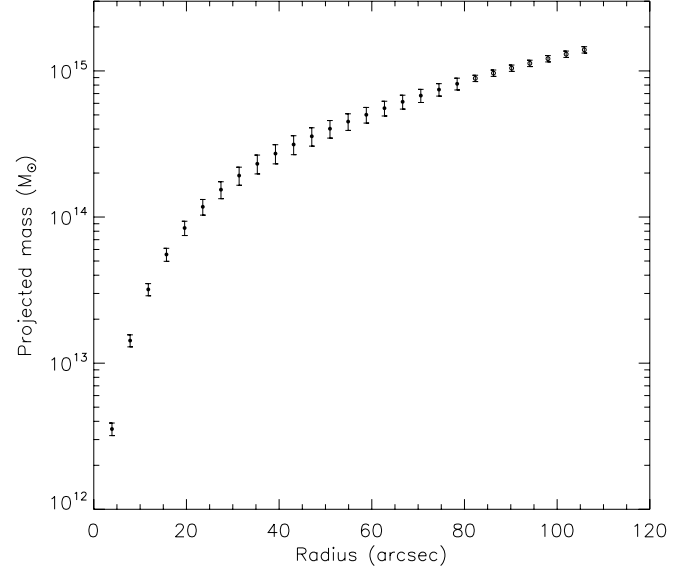


FIG. 12.—Projected mass in the cluster core. The mass is directly computed from the mass map in Fig. 8 by adding the mass pixel values within a given aperture (filled circle). At  $r \gtrsim 80''$  we cannot complete a circle within the field, and thus we assume an axisymmetry to extend the profile out to  $r \sim 110''$  (open circle).

Einstein radius is tightly constrained by the weak-lensing data. A detailed comparison between the model prediction and the observed shear profile is made in § 4.3.

The flat density profile of our model implies that projected cumulative masses rise steeply (Fig. 12). The projected mass within the radius of the  $z = 1.675$  arc ( $r \simeq 30''$ ) is often quoted for mass comparison between different mass models. Our model predicts a projected mass of  $M(r < 30'') = (1.79 \pm 0.13) \times 10^{14} M_\odot$ , which is consistent with the result of Broadhurst et al. (2000); when we reproduce their model in the current cosmology, we obtain  $M(r < 30'') \simeq 1.84 \times 10^{14} M_\odot$ . The result in Tyson et al. (1998) was obtained assuming the  $\Omega_M = 1$  flat universe. Nevertheless, when only the difference in  $h$  is considered in the transformation of the result, it also gives a similar mass of  $M(< 30'') \sim 1.6 \times 10^{14} M_\odot$ . This excellent agreement of the projected total masses within the radius of the arcs among different models is not surprising, however, because for an axisymmetric lens the mean mass density within an Einstein radius becomes unity regardless of the difference in the radial profile.

Ota et al. (2004) claim that their X-ray mass from the *Chandra* analysis is smaller than the lensing result by a factor of 3 at  $r = 35''$  in the  $\Omega_M = 1$  flat universe. The difference becomes somewhat reduced if the result is reproduced in the current cosmology and a slightly smaller aperture  $r = 30''$  is chosen. Under the hypothesis of hydrostatic equilibrium, the *Chandra* X-ray measurements of  $\beta = 0.71$  and  $T = 4.47$  keV from Ota et al. (2004) imply  $M(r < 30'') \sim 7.94 \times 10^{13} M_\odot$ , which is still lower than the lensing estimation by a factor of 2.

#### 4.3. Reduced Tangential Shears

The reduced tangential shear is defined as

$$g_T = \langle -e_1 \cos 2\phi - e_2 \sin 2\phi \rangle, \quad (25)$$

where  $\phi$  is the position angle of the object with respect to the cluster center and  $e_{1(2)}$  is the object ellipticity. Because each galaxy has its own intrinsic shape, the reduced shear can be estimated by taking azimuthal averages in radial bins  $\Delta r$ . Figure 13 shows the reduced tangential shears of Cl 0024+17 after the

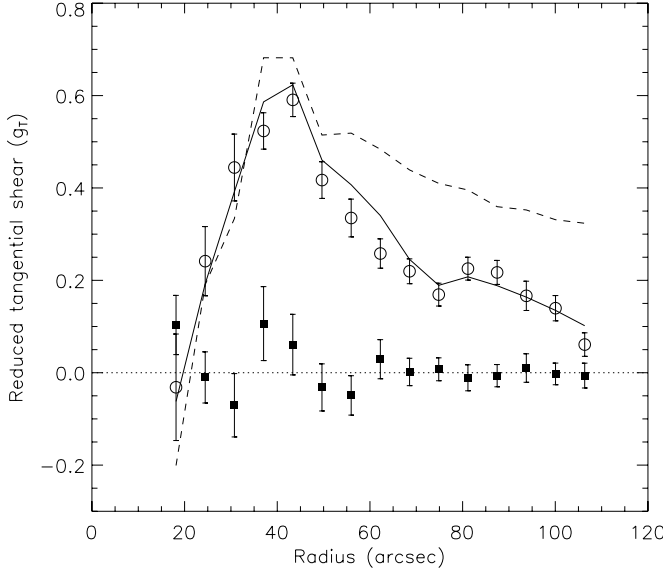


FIG. 13.—Reduced tangential shears of Cl 0024+17. Open circles represent the reduced tangential shears measured from  $\sim 1300$  background galaxies. We note that there is a dip at  $r \sim 75''$ , which indicates the presence of the ringlike substructure seen in the two-dimensional mass reconstruction or the bump in the radial density profile. We display the predicted shears estimated from our mass profile (solid line). Also shown are the predicted tangential shears when the Broadhurst et al. (2000) model is assumed (dashed line). We also performed the  $45^\circ$  rotation (*B-mode*) test to examine possible systematics. As observed (filled square), the lensing signal disappears in this case and the residual amplitudes are consistent with the statistical errors.

systematic underestimation is corrected for high shears (see Appendix A). The overall shape of the profile is consistent with our expectation for a typical axisymmetric lens. The background galaxies are most strongly stretched in the tangential direction near the Einstein radius and the tangential shears decrease for increasing  $r$ . Inside the Einstein radius, the tangential shear similarly goes down as  $r$  decreases. However, near the cluster center, the lensed images tend to become radially stretched. Hence, the observed shears must cross the zero line and become negative. Filled squares are the results from the  $45^\circ$  rotation (*B-mode*) test. The lensing signals disappear and the residual amplitudes are consistent with the statistical errors.

Also shown in Figure 13 are the predicted tangential shears from the Broadhurst et al. (2000) model (dashed line) and our result (solid line). These predicted values are estimated by placing circular objects at the location of the background galaxies; assuming the intrinsic ellipticity dispersion (eq. [20]), the expected errors of these points are similar to those of the observed points but are omitted for readability. The Broadhurst et al. (2000) model predicts tangential shears consistent with our observation at  $r \lesssim 40''$ , but much higher at  $r \gtrsim 40''$ . The discrepancy implies that their mass profile inside the Einstein radius is similar to our result, but steeper at larger radii; we already noticed this directly in the comparison of the radial density plot (Fig. 11). As the strong-lensing region used by Broadhurst et al. (2000) is limited only to the region interior to the Einstein radius ( $r \lesssim 30''$ ), their predicted shear profile is increasingly discrepant for  $r > 40''$ .

An interesting feature in this tangential shear plot is the dip present at  $r \sim 75''$ . It is clear that this feature reflects the ringlike substructure seen in the two-dimensional mass map (Fig. 8) or the bump in the radial density plot (Fig. 10). We stress that, as these data points are uncorrelated, the observed departure from a monotonic decrease is highly significant. It may not be intuitive, however, to understand why the bump in the radial density

profile appears as a dip in the tangential shear profile as the relation between mass density and reduced shear is complicated. For an axisymmetric lens, the reduced shear at  $r$  is given by

$$g(r) = \frac{\bar{\kappa}(<r) - \kappa(r)}{1 - \kappa(r)}, \quad (26)$$

where  $\bar{\kappa}(<r)$  is the average surface density within  $r$ . Using equation (26) along with the radial density plot (Fig. 10), it is possible to qualitatively reproduce the observed features in the shear profile despite the slight deviation of the Cl 0024+17 mass distribution from axisymmetry.

Kneib et al. (2003) presented a reduced shear profile of Cl 0024+17 at  $50'' < r < 1000''$  based on two passband (F450W and F814W) WFPC2 observations. In the overlapping ( $50'' \lesssim r \lesssim 100''$ ) region, we find that their shear profile is systematically lower than ours and the discrepancy is increasing for decreasing radius. We suspect that the difference mainly comes from the somewhat large dilution of the lensing signal from a non-background population in their source catalog. With only two passband WFPC2 data available, this contamination is inevitable. Furthermore, our ACS observations are much deeper than their WFPC data, allowing us to utilize more distant and more highly distorted galaxies that were not previously available (i.e., our effective source plane is at higher redshift). However, it is encouraging to observe that their shear profile also possesses a similar dip at  $r \sim 75''$  (see Fig. 7 of their paper).

#### 4.4. Source Image Reconstruction

The ability to correctly reproduce the observed multiple images is a necessary but not sufficient condition for a robust mass model, especially if the strong-lensing data are sparse. To put our model to the test, we regridded the  $50 \times 50$  deflection field into the  $3920 \times 3920$  grid (matching the resolution of the ACS WFC cluster image shown in Fig. 1) using bicubic interpolation and performed delensing of the well-known five multiple images at  $z = 1.675$ . The top panels of Figure 14 show the observed lensed images directly cut from Figure 1. In the bottom panels, we display the delensed image of each arc predicted from our deflection potential. It is apparent that the orientation, parity, and size of these delensed images are highly consistent with each other. Colley et al. (1996) presented the first source delensing of the three well-resolved arcs (corresponding to A1, A3, and A4 in our nomenclature) from the WFPC2 image analysis. Their reconstructed images have similar orientations (note that north is up in their image) and ellipticities to ours with identical parity. Nevertheless, the high sampling resolution of ACS and the improved mass modeling allow us to obtain the delensed images in greater detail.

We also examined the result alternatively by relensing one of these source images back to the image plane. Initially, the result was less than ideal, yielding more than the five known multiple images. The relensed images at the location of the five known arcs were in good agreement with the observation, whereas the rest of the predicted images at other locations look much less definite. Nevertheless, this result should not discredit the mass model because noise can cause the deflection field at any arbitrary location to coincidentally point to the same location. We were able to easily fix the problem manually by slightly perturbing the deflection potential of the region where *false* images were predicted. The resulting mass map looks virtually identical to the original one and the minimizing function  $f$  (eq. [14]) is as small as the initial value.

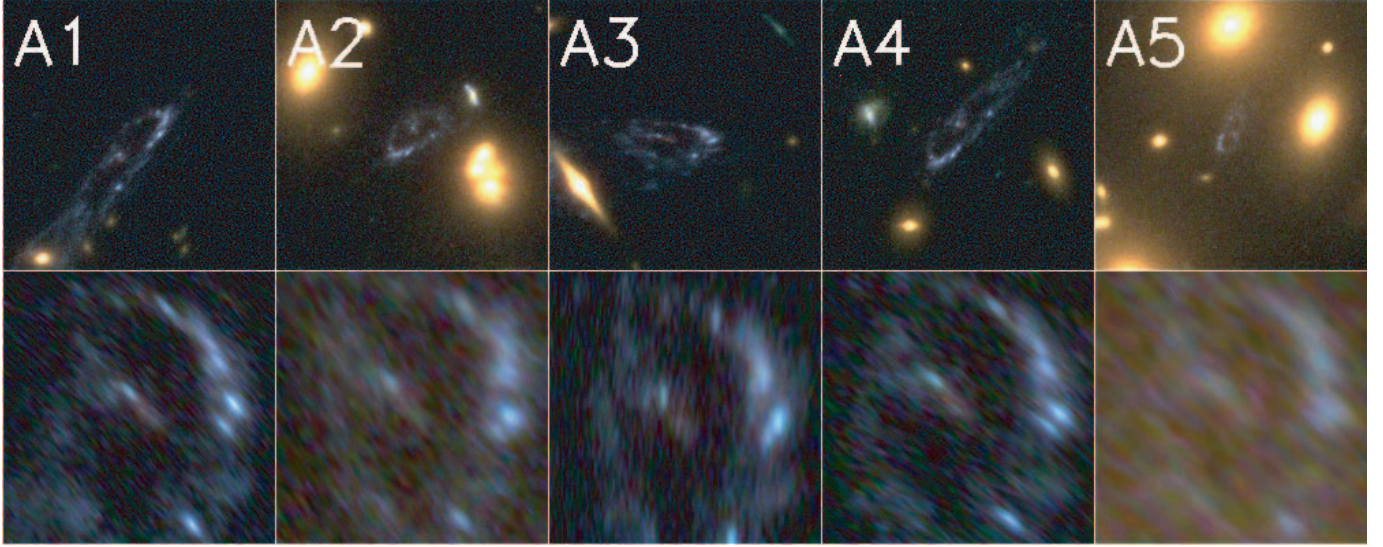


FIG. 14.—Source image reconstruction of the five well-known multiple images at  $z = 1.675$ . The top panels show the observed lensed images directly cut from Fig. 1. In the bottom panels, we display the delensed image of each arc predicted from our deflection potential. Note that the orientation, parity, and size of these delensed images are consistent with each other. The sizes of the delensed source images are approximately  $0.4'' \times 0.5''$ .

Because only their photometric redshifts are available with less distinctive morphology, we imposed only weak constraints on the two other multiple systems at  $z_{\text{phot}} = 1.3$  and  $2.8$  (§ 3.2). The delensed positions of B1–B2 at  $z_{\text{phot}} = 1.3$  agree nicely and their images in the source plane are similar to each other. We note that the source positions of C1–C2 are also close, yet slightly separated by  $\sim 40$  pixels ( $\sim 2''$ ); this makes the  $\chi^2_\mu$  values per constraint rather large for C1–C2 ( $\sim 3$ ), whereas they remain close to unity for A1–A5 and B1–B2.

When we forced the two locations to coincide in our mass reconstruction, the smoothness of the resulting mass map was compromised. Since the spectroscopic redshifts of the source are unknown, the solution obtained in this way cannot be claimed to be better, and thus we chose to accept the original result as our final mass model.

#### 4.5. Other Sources of Errors and Their Impacts

It is certain that we did not consider all sources of errors in our error analysis. Important among these are photometric redshift uncertainties and the large-scale structures in the ACS field of CI 0024+17.

Because lensing signals depend on all masses along the line of sight between the observer and sources, some large-scale structures in front of and behind the cluster can contribute to the lensing signals. In Jee et al. (2005b), we integrated the power spectrum from us to the effective source plane in order to estimate the contribution in the evaluation of the total mass of the high-redshift cluster MS 1054–0321 at  $z = 0.83$ . We found that the error introduced by this cosmic shear amounted to  $\sim 14\%$  of the total cluster mass within 1 Mpc. Therefore, it was a significant factor in the total error budget for that cluster. Since the similar formalism to compute the cosmic shear contamination has not been developed for the current mass reconstruction method, we do not attempt to estimate the corresponding errors for CI 0024+17. Nevertheless, we suspect that the cosmic shear-induced error is substantially smaller for the current study because the lens is at much lower redshift where the cluster lensing efficiency is much higher.

The typical uncertainty of  $\delta z \sim 0.1$  in photometric redshift estimation does not greatly affect the evaluation of the expected

reduced shear in equation (13). The cosmological weight function (eq. [9]) changes slowly with source redshift when the lens is at  $z = 0.4$ . Hence, the change in the expected ellipticity due to the uncertainty of  $\delta z \sim 0.1$  is much smaller than the intrinsic ellipticity dispersion in many cases.

What will happen to the cluster mass profile if the redshifts of the B1–B2 and C1–C2 systems that we used as strong-lensing constraints have significantly large photometric redshift errors ( $\delta z > 0.1$ ) and correct spectroscopic redshifts become available in the future? Because B1–B2 and C1–C2 are used to lift the mass-sheet degeneracy, the new mass map will be a simple invariant [ $\kappa \rightarrow \lambda\kappa + (1 - \lambda)$ ] transformation of the current mass map. Therefore, the overall shape of the mass profile and the significance of the ring feature at  $r \sim 75''$  will not be greatly affected. We also repeat that the transformation will not change the total projected mass within the Einstein radius.

Finally, despite the deep, six-passband ACS photometry and the use of HDF-N priors, we expect that there still is a small fraction of a nonbackground population in our source catalog due to some catastrophic errors in photometric redshift estimation. Because of the small ACS field and the lack of known spectroscopic sample for faint galaxies ( $i_{775} > 24$ ), it is difficult to estimate this fraction reliably. As we did not account for the dilution of the lensing signal from the contamination, one may argue that our mass estimates are lower limits. However, in the nonlinear lensing regime where we combine strong- and weak-lensing constraints, the effect is reversed. For example, if the contamination is removed somehow in our source catalog, the reduced shear profile (Fig. 13) will be shifted upward. The higher shear profile certainly implies a steeper mass profile in the nonlinear regime. Therefore, the cluster mass decreases more rapidly as  $r$  increases in this case.

## 5. DISCUSSION

### 5.1. Ringlike Structure as Direct Evidence of a Line-of-Sight Collision

The first observational indication that CI 0024+17 might have undergone a high-speed line-of-sight collision was presented by Czoske et al. (2002) based on their wide-field spectroscopic



survey of the cluster. Their redshift histogram obtained from the  $\sim 300$  spectroscopically confirmed cluster members shows that the redshift distribution of the cluster is bimodal; the larger peak is at  $\bar{z} = 0.395$  and the smaller peak at  $\bar{z} = 0.381$ . This bimodality becomes more distinct if the histogram is reproduced only using the cluster galaxies at  $r > 200''$ . On the other hand, when the redshift distribution at  $r < 200''$  is examined, the separation between the two peaks is not clear; it rather appears that there is one main clump at  $\bar{z} = 0.395$  yet skewed toward negative velocities. This unusual redshift distribution of the cluster led Czoske et al. (2002) to suggest a scenario wherein the system underwent a high-speed line-of-sight collision of two subclusters with a mass ratio of 2:1 a few Gyr ago, and the negative velocity tail and the smaller peak originally had belonged to the less massive system. They also supported their scenario with an  $N$ -body simulation, which predicts the observed velocity distribution.

We argue that the ringlike dark matter substructure and the flat density profile of Cl 0024+17 in our high-resolution mass reconstruction provide alternative yet much stronger evidence for the line-of-sight collision and can be used to refine the scenario of Czoske et al. (2002). A high-speed collision of two massive clusters can be approximated by a gravity impulse at the cluster center lasting  $\Delta t$ , whose order is the size of the cluster divided by the impact velocity. Because of an increased gravity, the two clusters contract for the duration of the impulse  $\Delta t$ . When the impulse is over, the contraction stops and both clusters start to expand. The extra kinetic energy causes the dark matter in the cluster outer regions to become unbound and to scatter to a large distance. The dark matter in the cluster inner regions will also expand. However, because it is still bound to the clusters, the expansion slows down. This deceleration leads to a crowding of orbits or a shell, which should appear as a ringlike structure around the cluster cores in projection.

One challenging question in the interpretation of the ripple-like structure is, however, how efficient the gravitational shock is on a cluster scale. The aforementioned ring creation mechanism is analogous to that in ring galaxies (Lynds & Toomre 1976). Quite a few numerical simulations have shown that the ringlike structure can arise from a radial density propagation in a high-speed collision of two galaxies (e.g., Hernquist & Weil 1993). Nevertheless, we need to examine if the argument for ring galaxies can also apply to a collision of two spheroids on a cluster scale.

To investigate the problem, we perform a purely collisionless  $N$ -body simulation of a collision of two massive clusters similar to the Czoske et al. (2002) experiment. The mass ratio is set to 2:1, and both clusters follow a softened isothermal distribution (i.e.,  $\rho \propto [1 + (r/r_c)^2]^{-2}$ ). The core radius of the larger cluster is 100 kpc and has a mass of  $6 \times 10^{14} M_\odot$  within a 2 Mpc radius, whereas the core radius is chosen to be 60 kpc for the smaller cluster with  $3 \times 10^{14} M_\odot$  within a 1 Mpc radius. The number of particles for the larger and smaller clusters is  $2 \times 10^5$  and  $10^5$ , respectively; thus, a particle mass is  $3 \times 10^9 M_\odot$ . The initial separation is 3 Mpc with a relative velocity of  $3000 \text{ km s}^{-1}$ . A Plummer force softening length is set to 5 kpc. Note that although our choice of these parameters may resemble the hypothesized two clusters of Cl 0024+17 before the collision, we do not elaborate to refine them to ensure the desired final result. Our main goal here is to examine whether the observed density structure can occur in a purely collisionless encounter of two massive clusters. The simulation was carried out with the publicly available GADGET-2 software (Springel 2005) in a Newtonian space. The forces were computed through the tree algorithm.

We present four snapshots of the  $N$ -body simulation in Figure 15 at 0.5 Gyr intervals from the  $t = 0$  impact moment to  $t = 1.5$  Gyr after the core pass-through. In the  $t = 0.5$  Gyr snapshot, the cores of both clusters start to expand and the radial density profile plot shows the resulting disruption. We can also observe the cluster outer regions start to stream radially. At  $t = 1$  Gyr, the two cluster cores are separated by  $\sim 3$  Mpc, and it is clear that the slowing down of the expanding particles causes the formation of shell-like structures around both cores. The shells are rather flattened perpendicular to the collision axis and appear as ringlike structures when projected along the collision axis. The radial profile also shows a corresponding peak at  $r = 0.6$  Mpc. About 1.5 Gyr after the core passage, the shell-like structures are still present and expanding. We observe that these features last even after a few Gyr. By iterating the above simulation with different initial conditions (e.g., replacing the softened isothermal halos with cuspy profiles), we verify that these qualitative mass structures are somewhat ubiquitous in high-speed collisions although the details differ. We stress that the shells also arise for moderately off-center collisions. The ringlike structure and the small bump in the radial density profile seen in Figure 15 resemble the two-dimensional mass map (Fig. 8) and the radial mass profile (Fig. 10) of Cl 0024+17, respectively. Many factors determine the radius of the ring in the simulation as a function of the elapsed time, including mass ratios, core radii, impact velocities, etc. Nevertheless, we speculate from the dissipation of the shock in the X-ray observation and the size of the observed ring in our mass map that the two clusters in Cl 0024+17 collided perhaps 1–2 Gyr ago.

The exact representation of the mass structure of Cl 0024+17 requires fine-tuning of the initial conditions with the inclusion of the cluster ICM and will be a subject of future investigations. The numerical simulation of cluster mergers by Ricker & Sarazin (2001) included both dark matter and gas particles. Their head-on merger simulation with a 1:3 mass ratio demonstrates that both the dark matter and the gas components of the clusters survive the core passage and reach their maximum separation in a timescale of sound crossing time ( $\sim 1.9$  Gyr) although the gas components suffer severe distortions and thus are slightly displaced from the corresponding dark matter halos. Since their analyses were focused on the global X-ray properties of the merging clusters, the time evolution of the detailed dark matter profile was not investigated. Nevertheless, it appears that shell-like features are absent in their snapshots of the merger simulation. We suspect that the employed particle-mesh (PM) force computation did not provide the resolution and may have smoothed out small-scale features.

Having discussed the possible scenario for the formation of the ringlike structure with the numerical simulation above, we now consider two issues relating to the observational features of the ringlike structure. First, we note that there are azimuthal variations in the observed “ring.” The feature appears to be strongest in the lower left (southwest) quadrant and weakest in the upper left (southeast) corner. Obviously, the mass distributions in real clusters are not symmetric. Hence, the ring arising from the collision should reflect somehow the previous asymmetry. In addition, as already mentioned above, moderately off-axis collisions produce similar structures. As a matter of course, in these cases the resulting ring has azimuthally varying densities. Furthermore, the noise in our mass reconstruction can perturb the already existing azimuthal density variation; the number density of background galaxies is not uniform over the cluster field.

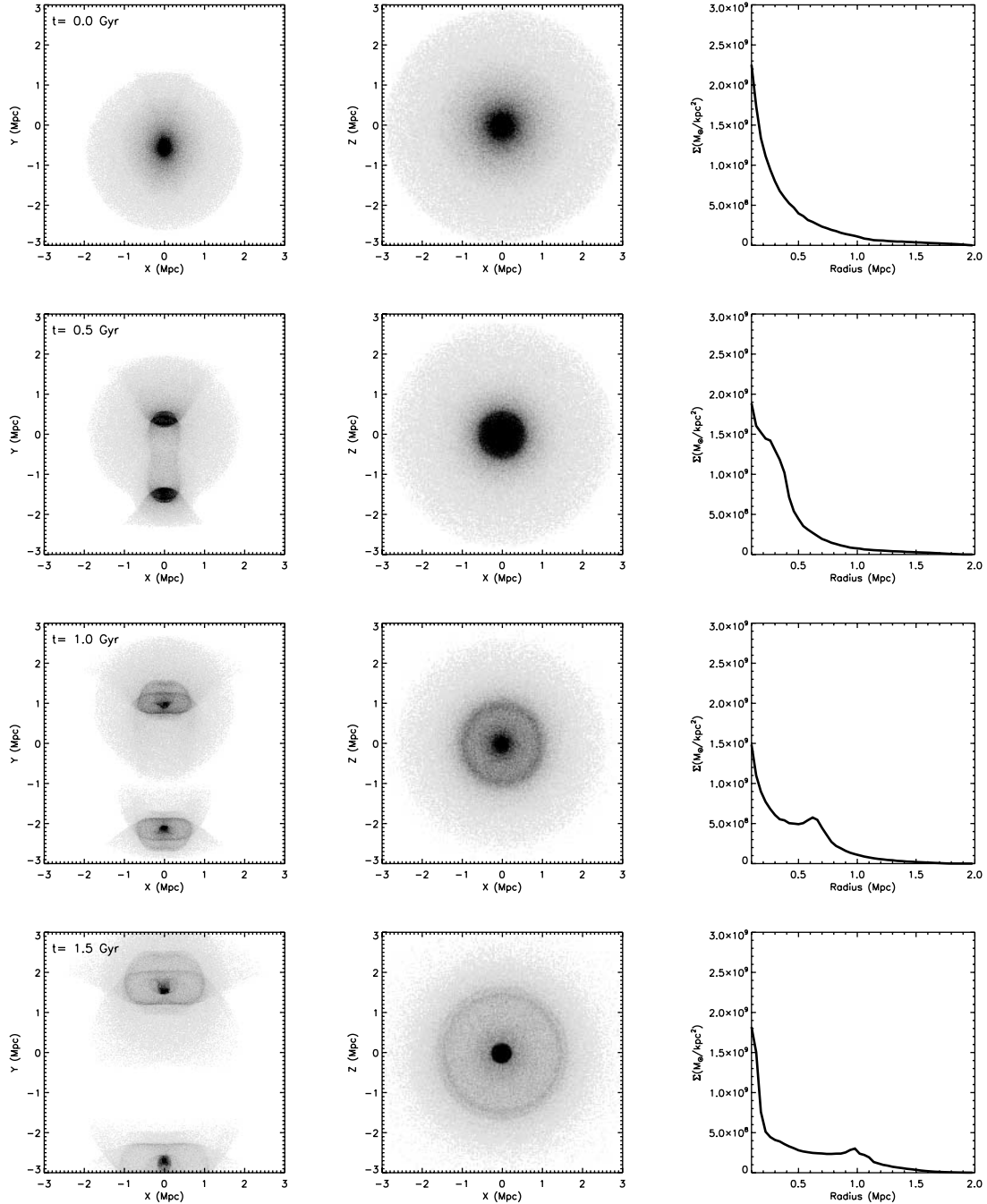


FIG. 15.—Numerical simulation of two colliding clusters. The mass ratio is set to 2:1, and both clusters follow a softened isothermal distribution (see text for parameters). Each row shows snapshots of the collisionless  $N$ -body simulation at a given epoch ( $t$  is an elapsed time since the core impact). Particle distribution is projected onto the  $x$ - $y$  plane (*left*; the plane containing the collision axis) and the  $x$ - $z$  plane (*middle*; viewed along the collision axis). We also illustrate the projected ( $x$ - $z$  plane) density profile in the right column. A radially expanding shell is visible in the snapshots  $\sim 1$  Gyr after the core impact, which also produces a prominent bump in the radial mass profile.

Second, in the comparison of the mass contours with the smoothed cluster light distribution in Figure 9b it appears that the overall ringlike structure is not well traced by the cluster galaxies although we observe that there are some scattered groups of galaxies, which seem to slightly enhance the local density contrast. The nice agreements between cluster light and mass in our previous investigations (Jee et al. 2005a, 2005b) being acknowledged, this may seem surprising at first. However, considering that the cluster galaxies would sample the underlying dark matter halo only sparsely and the density contrast in the ringlike structure (presumably projection of the lower contrast

three-dimensional shell-like structure) is low, we should not expect to see substantial crowding of the cluster galaxies in the  $r \sim 75''$  annulus.

### 5.2. The ICM Profile and Resolving the Mass Discrepancy

The global X-ray temperature  $T = 4.47^{+0.83}_{-0.54}$  keV of Cl 0024+17 obtained from the *Chandra* data (Ota et al. 2004) is slightly higher than the *XMM-Newton* measurement  $T = 3.52 \pm 0.17$  keV (Zhang et al. 2005). We investigate the possibility that the most recent calibration of the *Chandra* instrument, especially in the time-dependent gain and the low-energy quantum efficiency

degradation corrections, may produce some appreciable shift in the temperature measurement. We reanalyze the archival *Chandra* observation of the cluster with the *Chandra* Interactive Analysis of Observations (CIAO) software version 3.3 and the Calibration Database (CALDB) version 3.2, following the procedure detailed in Jee et al. (2005b, 2006). Using the same cluster aperture and background annulus defined by Ota et al. (2004), we obtain  $T = 4.25^{+0.40}_{-0.35}$  keV and  $Z = 0.74^{+0.24}_{-0.21} Z_{\odot}$ . Our measurements are consistent with the results of Ota et al. (2004), and the improved understanding of the *Chandra* instrument does not seem to affect the temperature measurement of the cluster in this case. However, we suspect that the difference between the *Chandra* and the *XMM-Newton* measurements originates from some systematic discrepancy in the two instrument calibrations; we observed that our X-ray temperature determination of the high-redshift cluster MS 1054–0321 from the *Chandra* data (Jee et al. 2005b) has a similar amount of shift in the same direction with respect to the result from the *XMM-Newton* data analysis (Gioia et al. 2004).

Why is the temperature of the cluster so low? Under the hydrostatic equilibrium assumption the mass of the cluster predicted from the X-ray temperature, even with the highest estimate of  $\sim 5.7$  keV by Soucail et al. (2000) from the *ASCA* observations, cannot explain the strong-lensing features (i.e.,  $\kappa < 1$ ). Are we observing the ICM significantly disrupted from the merger shock? Both the relaxed appearance of the X-ray emission and the low temperature of the cluster suggest that we might not be observing the most violent phase of the collision as in the case of the “bullet” cluster 1E 0657–56 at  $z = 0.3$  (Markevitch et al. 2002), which shows an average temperature of 14–15 keV with a large spatial variation of temperature and gas density. Markevitch et al. (2002) argue that the two subcluster cores in 1E 0657–56 passed through each other nearly in the plane of the sky 0.1–0.2 Gyr ago at a supersonic speed of 3000–4000 km s $^{-1}$  and the ICM peaks have been swept back due to the ram pressure. When the mean velocity difference of  $\sim 3000$  km s $^{-1}$  between the foreground and the main clusters of Cl 0024+17 is considered, it is plausible that we might be looking at a similar event, yet along the collision axis at a much later epoch. The merger shocks that once heated the ICM of Cl 0024+17 to  $\gtrsim 10$  keV would have been dissipated in a timescale of 1–2 Gyr.

One critical question in this scenario is whether the ICMs of the two subclusters have merged already and settled down to a single X-ray system or have survived the collision with a distinct separation. Ota et al. (2004) and Zhang et al. (2005) treated Cl 0024+17 as a single X-ray system in their X-ray analyses although Ota et al. (2004) demonstrated that the ICM profile can be better described by two isothermal  $\beta$  models. The inadequacy of a single  $\beta$  model in Cl 0024+17 is also seen in our reanalysis of the *Chandra* data (Fig. 16). The surface brightness (open circle) is measured from the exposure-corrected *Chandra* image after the known point sources are removed. The dashed line represents the X-ray surface brightness only when a single isothermal  $\beta$  model is fitted, giving  $\beta = 0.51 \pm 0.02$  and a core radius of  $r_c = 31'' \pm 3''$  with  $\chi^2/\text{dof} = 1.79$ . As shown by the solid line, the overall ICM profile is much better represented by a superposition of two isothermal  $\beta$  models ( $\chi^2/\text{dof} = 1.03$ ). Following the argument of Ota et al. (2004), we froze  $\beta$  of one component to unity as any value in the neighborhood of one does not substantially alter the goodness of the fit. The core radius of this component with  $\beta = 1$  is estimated to be  $r_c = 13'' \pm 2''$ , whereas  $\beta = 0.67 \pm 0.06$  and  $r_c = 60'' \pm 9''$  are obtained for the other component. This significant improvement in the goodness of fit motivates us to consider the hypothesis that we might be observing two X-ray systems aligned along the line of

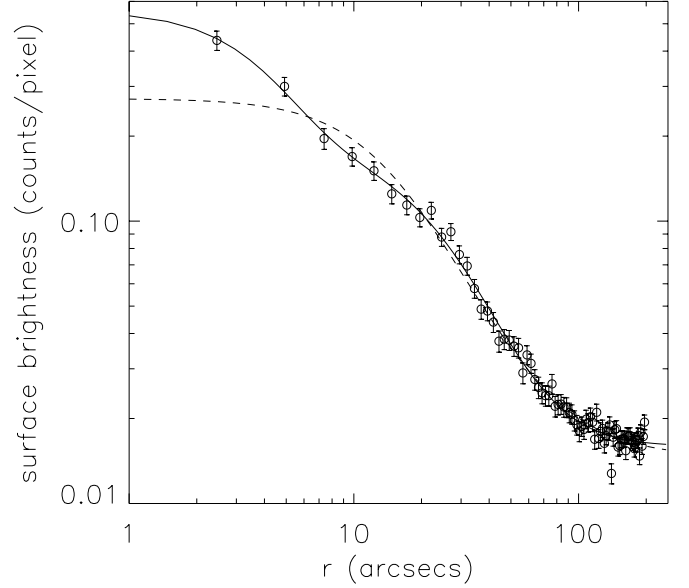


FIG. 16.—X-ray surface brightness of Cl 0024+17 obtained from the exposure-corrected *Chandra* image. The azimuthally averaged X-ray profile (open circle) cannot be well approximated by a single isothermal  $\beta$  model (dashed line); the best-fit values are  $\beta = 0.51 \pm 0.02$ ,  $r_c = 31'' \pm 3''$ , and  $\chi^2/\text{dof} = 1.79$ . The solid line is the result when two isothermal  $\beta$  models are fitted simultaneously while freezing the slope of one system to unity. The core radius of this component with  $\beta = 1$  is estimated to be  $r_c = 13'' \pm 2''$ , whereas  $\beta = 0.67 \pm 0.06$  and  $r_c = 60'' \pm 9''$  are obtained for the other component. The two-component model gives a significantly better fit to the observed surface brightness with  $\chi^2/\text{dof} = 1.03$ .

sight, in which case the cluster mass must be the sum of the two components.

The projected cluster mass within a cylindrical volume for a given temperature,  $\beta$  index, and core radius  $r_c$  can be estimated by (Ota et al. 1998; Jee et al. 2005b)

$$M(r) = 1.78 \times 10^{14} \beta \left( \frac{T}{\text{keV}} \right) \left( \frac{r}{\text{Mpc}} \right) \frac{r/r_c}{\sqrt{1 + (r/r_c)^2}} M_{\odot}. \quad (27)$$

Because no appreciable temperature gradient is detected, we assume that the two components have an identical temperature of  $T = 4.25^{+0.40}_{-0.35}$  keV, but different core radii and slopes  $\beta$  as estimated above. Within the radius of the arc  $r = 30''$ , the sum of the two components from equation (27) is a total of  $1.5 \times 10^{14} M_{\odot}$ , which is impressively close to our lensing estimation  $\sim 1.79 \times 10^{14} M_{\odot}$ . Although one can adjust the value of the fixed parameter  $\beta$  from unity or change the temperature ratio of the two components in order to improve the agreement, we do not attempt the investigation here.

The survival of X-ray systems from a high-speed collision is seen in cluster merger simulations. As mentioned in § 5.1, the simulated X-ray clumps survive equal-mass mergers and their cores persist even a few Gyr after the core passage (Ricker & Sarazin 2001). The *Chandra* X-ray observation of the bullet cluster 1E 0657–56 provides observational support for the survival of merging X-ray cores. Although offset from the corresponding dark matter clumps and cluster galaxies, the two distinct X-ray systems supposedly moving away from each other are witnessed in the *Chandra* X-ray image (Markevitch et al. 2002). Once two X-ray cores survive a high-speed collision as in this example, they will be dragged and separated further by the corresponding dark matter clumps, the gravitationally dominant components of the cluster. How the two survived X-ray systems

will behave under the influence of the dark matter halo afterward is still an open question. Nevertheless, we suspect from their collisional nature and the results presented here that the cluster ICMs tend to relax faster than the hosting halo with some small-scale structures smeared out.

### 5.3. Direct Evidence of Dark Matter and Prospects of Constraining Dark Matter Particle Cross Section

Clowe et al. (2004) detected significant dark matter centroid offsets with respect to the ICM centroids in 1E 0657–56 from a ground-based weak-lensing analysis. They used them as an argument about the existence of dark matter. Similar offsets were also observed in the weak-lensing analyses of two high-redshift clusters, Cl 0152–1357 and MS 1054–0321, based on *HST* ACS data (Jee et al. 2005a, 2005b). It is hard to explain these offsets in the Modified Newtonian Dynamics (MOND) paradigm (Milgrom 1983) without dark matter, which predicts that the mass concentrations coincide with the ICM clumps, the dominant mass component of the cluster in the absence of dark matter (however, see Moffat 2006).

The ringlike mass structure at  $r = 0.4$  Mpc surrounding the dense core at  $r \lesssim 0.25$  Mpc not traced by the cluster ICM nor by the cluster galaxies serves as the most definitive evidence from gravitational lensing to date for the existence of dark matter. If there is no dark matter and the cluster ICM is the dominant source of gravity, the MONDian gravitational lensing mass should follow the ICM, which, however, does not show any hints of such peculiar mass distribution. The absence of the ringlike structure in the *Chandra* X-ray image is consistent with our current understanding of the collisional nature of an ICM.

Although originally hypothesized as collisionless, dark matter particles are now commonly proposed to possess nonnegligible self-interacting cross sections. Self-interacting dark matter particles reconcile some discrepancies between the simulated and observed halo structures (i.e., cuspieness of the central profile and overprediction of dwarf halos by simulations). The heat conduction propagated by self-interaction of dark matter particles not only reduces the cuspieness of the cold dark matter simulation but also prevents the overprediction of subhalos. Observational constraints on self-interacting cross sections of dark matter particles can be made by a variety of methods (e.g., Spergel & Steinhardt 2000; Miralda-Escude 2002; Gnedin & Ostriker 2001; Furlanetto & Loeb 2002; Hennawi & Ostriker 2002; Natarajan et al. 2002; Markevitch et al. 2004).

The central density profile of Cl 0024+17 has often been used as an argument for self-interacting dark matter (e.g., Spergel & Steinhardt 2000; Hogan & Dalcanton 2000). Apart from the controversy over whether or not gravitational lensing can indeed test the cuspieness of the cluster mass profile, the line-of-sight collision scenario originally proposed by Czoske et al. (2002) and supported by the current study, however, poses an important problem with the approach. Instead, the hypothesized collision history of Cl 0024+17 can provide an alternative and perhaps much stronger method to infer the nature of dark matter. The results of detailed hydrodynamic simulations including both collisional and collisionless particles can be compared with the current high-resolution mass map, the *Chandra* X-ray data, and the spectroscopic catalog of the member galaxies. The line-of-sight configuration is both good and bad news at the same time. It is good news because we are certain that the two clusters passed through the densest regions of each other. This crucial information is not directly available if the collision has occurred in the plane of the sky and the impact parameter must be assumed based

on observed features. In addition, the spectroscopically measured line-of-sight velocity difference of  $\sim 3000 \text{ km s}^{-1}$  between the two clusters of Cl 0024+17 can be safely assumed to represent their relative velocity. The bad news is that we cannot measure the offsets between the cluster galaxies, the X-ray clumps, and the dark matter centroids, which can potentially reveal the different hydrodynamic nature of the three cluster components.

Even without performing the detailed simulations suggested above, however, the mere detection of the ringlike dark matter structure leads us to suspect that presumably collisional cross sections of dark matter particles are either zero or much smaller than the cross sections of the plasma. Otherwise, as mentioned above, the shell-like features should have been erased 1–2 Gyr after the core impact.

## 6. SUMMARY AND CONCLUSIONS

We have presented a comprehensive, parameter-free mass reconstruction of Cl 0024+17 combining both strong- and weak-lensing data. The deep, six-passband ACS images of the cluster allow us to obtain a total of  $\sim 1300$  background galaxies whose shapes and photometric redshifts are reliably measured. These individual galaxies are highly distorted by the cluster's gravity and indicate the local reduced shears even without being smoothed over a large area. On the other hand, the well-known multiple-image system at  $z = 1.675$  and the two additional multiple-system candidates at  $z_{\text{phot}} = 1.3$  and  $2.8$  tightly constrain the inner structure of the cluster on an absolute scale, breaking the mass-sheet degeneracy. The resulting mass reconstruction from this dense distribution of the lensing signals is striking. It reveals the  $r \sim 0.4$  Mpc ringlike dark matter structure surrounding the dense core ( $r \lesssim 50''$ ). This peculiar substructure is not traced by the ICM nor by the cluster galaxies. Although offsets between dark matter and X-ray plasma in clusters were detected in the past, this clear discrepancy in distribution between dark matter and cluster galaxies has not been reported so far. The ring is visible even when we repeat the mass reconstruction without the strong-lensing data and the significance of the feature is very high ( $\sim 5$  and  $\sim 8 \sigma$  in the two-dimensional and the one-dimensional profile, respectively).

The most probable cause of the morphology is a high-speed line-of-sight collision of two massive clusters 1–2 Gyr ago, as also indicated by the bimodality of the velocity distribution. With a high-resolution collisionless  $N$ -body simulation, we demonstrate that the ringlike structure can arise by radially expanding, decelerating dark matter shells that once comprised the precollision cores. The shells (and thus the projected ringlike structure) are observed to last even a few Gyr after the core pass-through.

The large mass discrepancy of Cl 0024+17 between X-ray and lensing has been a long-standing puzzle. The high-speed collision scenario by Czoske et al. (2002) was acknowledged by Ota et al. (2004) and Zhang et al. (2005) in their X-ray analysis of the cluster. However, both papers still treat the X-ray emission as originating from a single merged system representing the global properties of the cluster, and they attribute the mass discrepancy to a departure from hydrodynamic equilibrium. In contrast, we suggest the possibility that the two X-ray systems survive the high-speed collision and are still separated as supported by cluster merger simulations (e.g., Ricker & Sarazin 2001). In this case, we are looking at a superposition of two X-ray systems. We interpret the unusual X-ray surface brightness distribution that can be explained by a superposition of two different isothermal profiles as indicating this possibility. The cluster mass derived

from the *Chandra* data with this hypothesis is  $\sim 1.5 \times 10^{14} M_{\odot}$ , consistent with the lensing result  $\sim 1.79 \times 10^{14} M_{\odot}$ .

Adopting the above scenario, CI 0024+17 is a very useful laboratory where many outstanding questions in astrophysics can be addressed. In particular, the cluster can serve as an excellent test bench for the hypothesized collisional dark matter study. The dark matter distribution obtained in the current study along with the X-ray observations and the extensive spectroscopic survey catalog will allow us to resolve many ambigu-

ities in initial parameter settings of comprehensive numerical simulations.

We acknowledge very detailed, helpful comments from the anonymous referee, which certainly improved the quality of the paper. ACS was developed under NASA contract NAS5-32865, and this research was supported by NASA grant NAG5-7697.

## APPENDIX A

### SHEAR RECOVERY TEST

We define the ellipticity of an object as  $e = (a - b)/(a + b)$ , where  $a$  and  $b$  are the major and minor axes, respectively, of an elliptical Gaussian function best describing the object in the least-squares sense. This definition was originally proposed by Bernstein & Jarvis (2002), and the algorithm was implemented by measuring the amount of shear necessary to make the object round in shapelets. Although the implementation works successfully in weak-lensing regimes (e.g., Jee et al. 2005a, 2005b, 2006), we find that the shapelet decomposition of a highly elongated object creates some artifacts such as Airy-like ringing as demonstrated in Figure 5. This is because the shapelet basis functions are built on *circular* Gaussian functions and thus inefficient in describing objects with high ellipticity. Therefore, in the current paper, we implement the algorithm by directly fitting a PSF-convolved elliptical Gaussian to measure the object ellipticity. The scheme is identical to the one used in GALFIT software (Peng et al. 2002) and also similar to IM2SHAPE (Bridle et al. 2002), which uses a sum of Gaussians to fit the object shapes.

We created artificially sheared images by lensing the Ultra Deep Field (UDF) parallel field (Thompson et al. 2006) with the singular isothermal sphere (SIS) model (Fig. 17). Because our aim is to investigate whether our ellipticity measurements can recover the input shear, this specific choice of the lens model should not bias our results. These artificially lensed images are then convolved with the ACS WFC PSF to simulate the seeing effect. We needed to iterate the procedure several times by varying the Einstein radii and the SIS center to increase the number of objects in our sample and to reduce the systematics potentially introduced by the intrinsic alignment of galaxies in the UDF parallel field.

If our ellipticity measurement  $\epsilon$  is indeed an unbiased estimate of the local reduced shear  $g$ , the average  $\langle \epsilon \rangle$  over a sufficient number of galaxies must converge to  $g$  (or  $1/g^*$  if  $|g| > 1$ ). However, in a critical lensing regime where the scale length of the variation of the lensing distortion is not much larger than object sizes, the ellipticity measurement is subject to underestimation in part because the objects become curved.

This systematic error can be noted in our comparison of the input shears with the output shears (Fig. 18). The plot demonstrates that the input reduced shear is well recovered up to  $g_{\text{in}} \sim 0.4$ , yet increasingly underestimated for higher distortion. Unless corrected for, this systematic underestimation biases the reconstructed mass profile of a cluster. The correction factors also largely depend on object sizes and magnitudes. We determine the values for different object sizes and input shears from this simulation and apply them to the

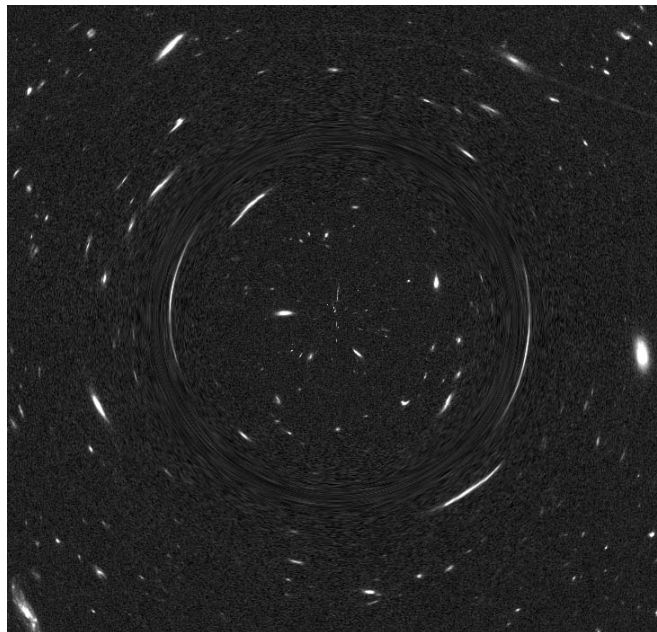


FIG. 17.—Example of a lensing simulation. We artificially lensed the UDF parallel field by placing an SIS model in front of it. The result is then convolved with the ACS WFC PSF to mimic the seeing effect. Because the UDF galaxies may possess intrinsic alignment due to some unknown large-scale structures, we iterate this procedure several times by altering the location of the SIS center and the Einstein radius.

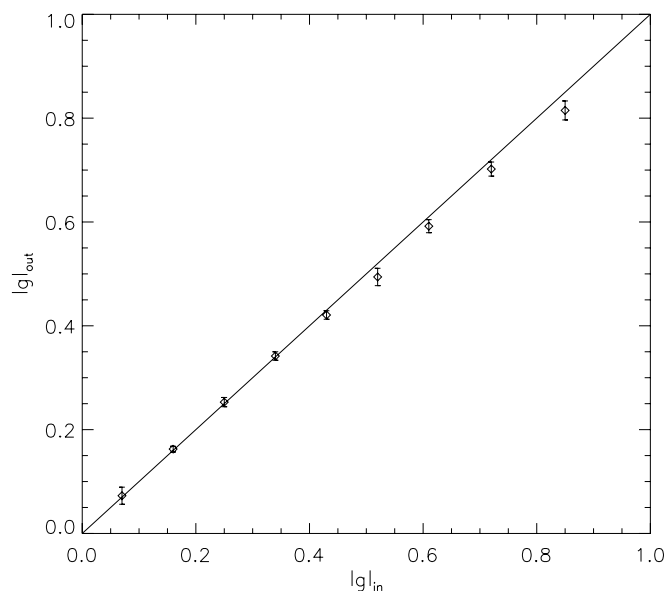


FIG. 18.—Shear recovery test from lensing simulation. The input shear  $g$  is accurately recovered until  $g_{\text{in}}$  reaches  $\sim 0.4$ , beyond which the object ellipticities systematically underrepresent the input shear  $g_{\text{in}}$ . We determined the required correction factors in this regime and used them to correct our measurements.

expected reduced shear  $g$  in equation (8). Because the local shear is unknown prior to iteration, one cannot apply the correction directly to the object ellipticity.

## APPENDIX B

### ESTIMATION OF ELLIPTICITY DISPERSION

For a given reduced shear  $\hat{g}$ , the dispersion of the observed ellipticities is often approximated as

$$\sigma_{\epsilon}(\hat{g}) = \sigma_{\epsilon}(0)(1 - \hat{g}^2), \quad (\text{B1})$$

where  $\sigma_{\epsilon}(0)$  is the intrinsic ellipticity dispersion before lensing occurs. Because this equation is derived under the assumption that the observed ellipticity distribution is Gaussian, we need to compare the equation with image simulation results. We utilize the results from the shear recovery simulation in the previous section in order to estimate the observed ellipticity distribution numerically. We selected objects whose magnitudes and colors are similar to the ones in our source sample and calculated their ellipticity deviation

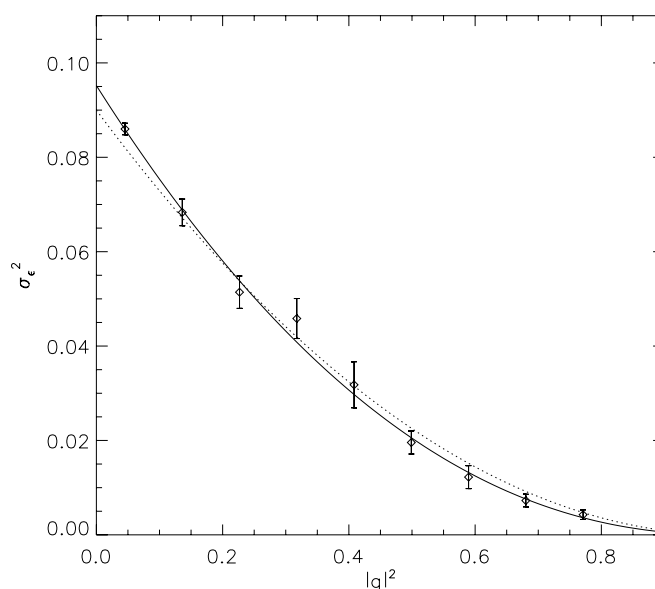


FIG. 19.—Estimation of ellipticity dispersion. The artificially lensed galaxy ellipticities  $\epsilon$  in the UDF parallel field are compared with the input shear  $g$ , and the difference  $\epsilon - g$  is used to calculate the dispersion  $\sigma_{\epsilon}^2$  (diamonds). This simulation result is reasonably well described by the conventional form  $\sigma_{\epsilon}(\hat{g}) = \sigma_{\epsilon}(0)(1 - \hat{g}^2)$  with  $\sigma_{\epsilon}(0) \simeq 0.3$  (dotted line) although it slightly underestimates (overestimates) the dispersion  $\sigma$  for small (large) values of  $\hat{g}$ . We use the analytic approximation of the simulation result  $\sigma_{\epsilon}(\hat{g}) = 0.31(1 - \hat{g}^2)^{1.11}$  (solid line) in our mass reconstruction.

from the expected value  $|e - \hat{g}|$  after the systematic underestimation for a high shear is corrected. We show the resulting relation between the input reduced shear  $\hat{g}$  and the measured ellipticity dispersion  $\sigma_e(\hat{g})$  in Figure 19. Note that the above equation with  $\sigma_e(0) \sim 0.3$  is a good approximation over a wide range of  $\hat{g}$  (*dotted line*). Nevertheless, it slightly underestimates the true dispersion at low  $\hat{g}$  and overestimates the value at high  $\hat{g}$ . We find that the numerical simulation result is better described by  $\sigma_e(\hat{g}) = 0.31(1 - \hat{g}^2)^{1.11}$  (*solid line*).

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